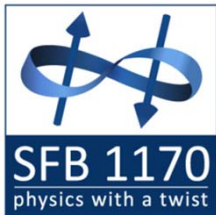
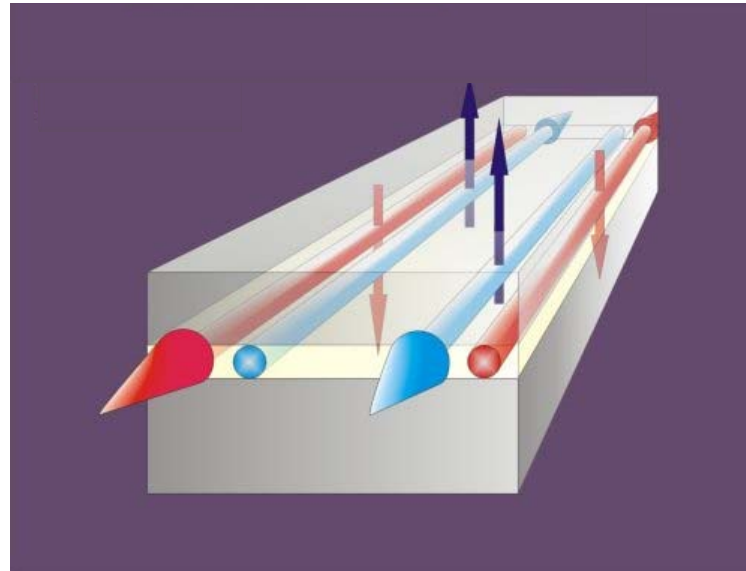


Dilute Magnetic Topological Insulators

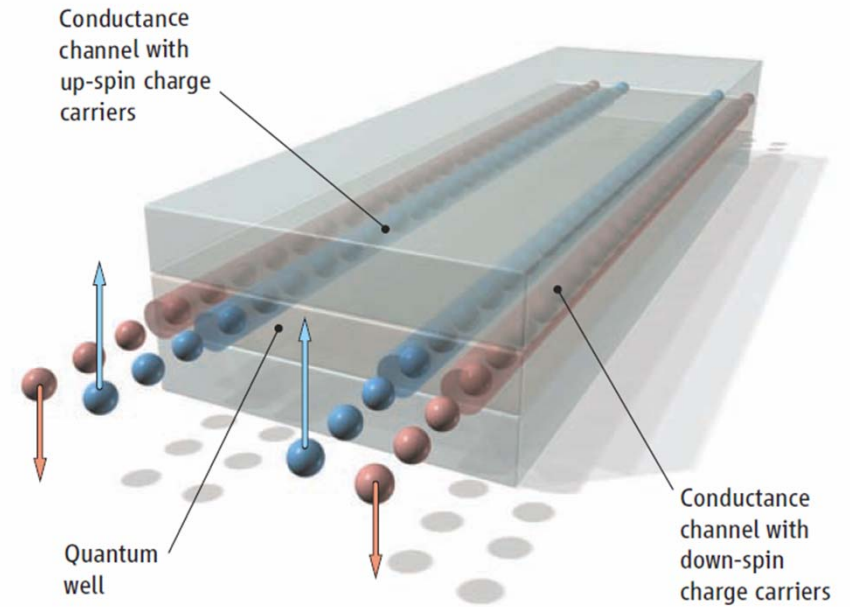
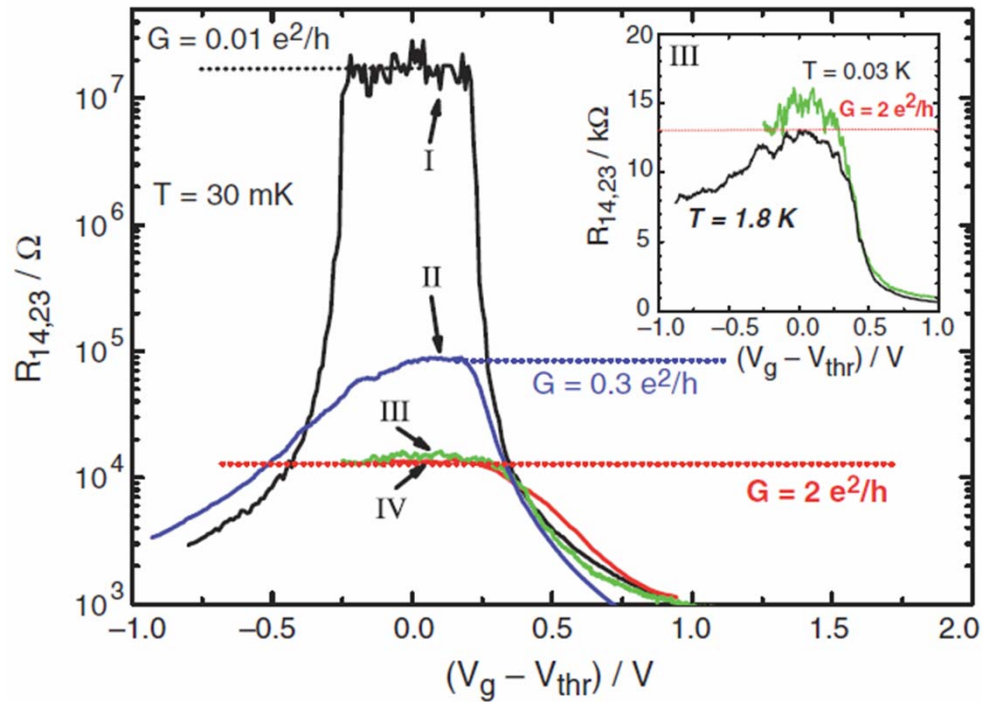
Laurens W. Molenkamp



EP III and Institute for Topological Insulators
Würzburg University

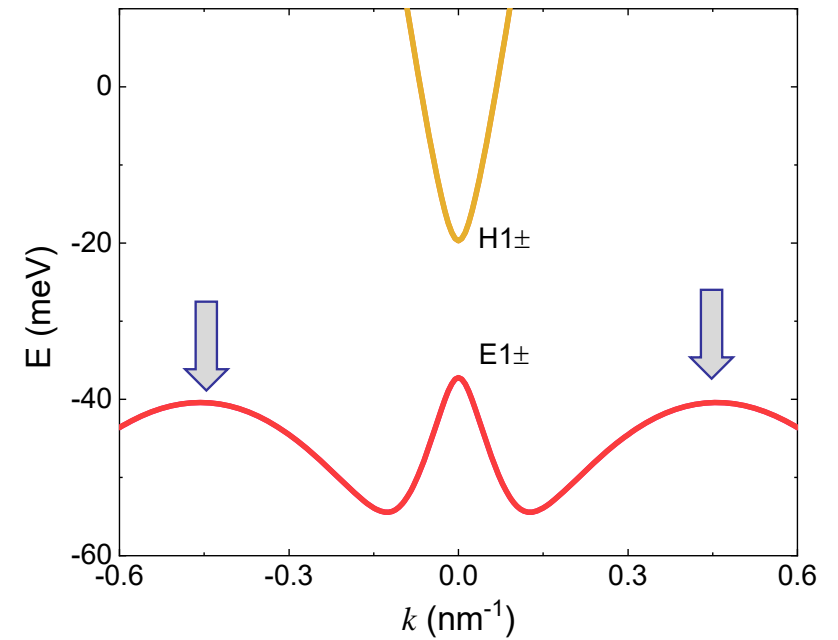
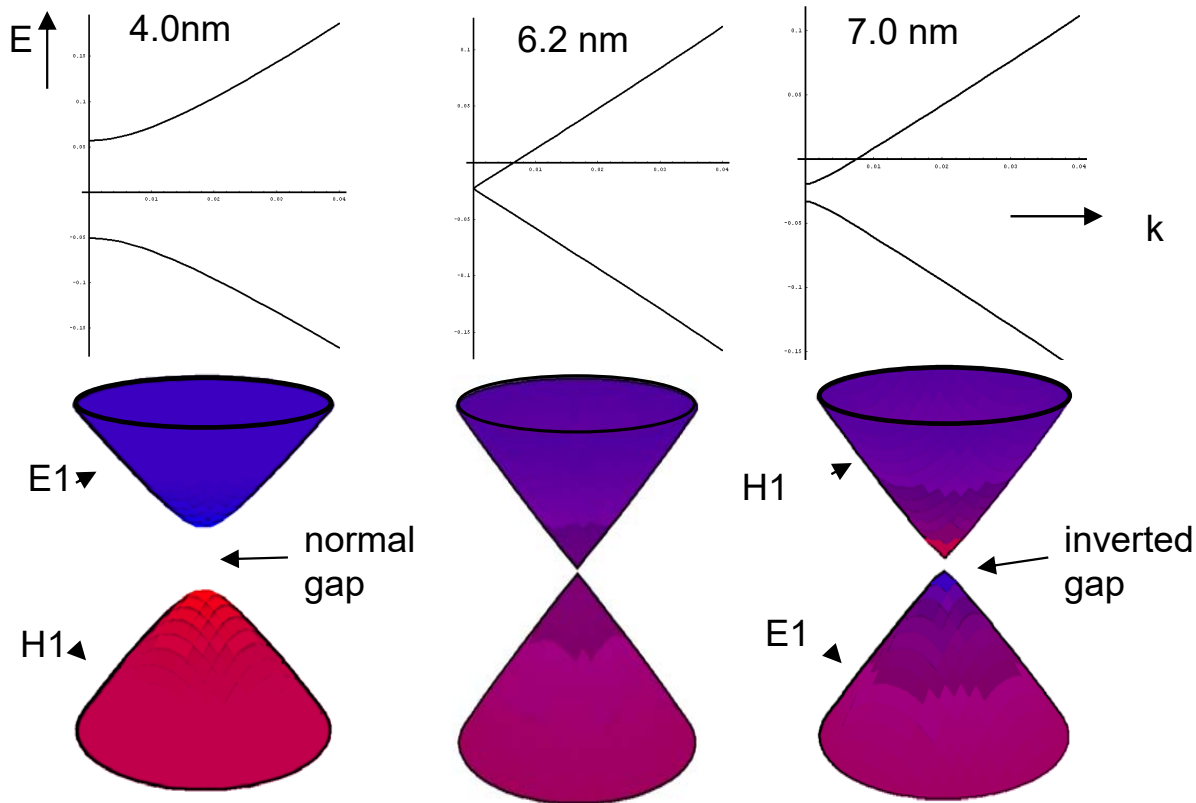


- HgTe quantum wells alloyed with Mn atoms
- Quantized spin Hall conductance in Mn-doped HgTe: Kondo screening
- Emergent quantum Hall phenomena
 - ✓ QSH states when time reversal symmetry is broken
 - ✓ Effect of enhanced DOS in valence band
- In 3-D TI: parity anomaly
- Proximitized layers: FFLO-type superconductivity



Some recent insights....

B.A Bernevig, T.L. Hughes, S.C. Zhang, Science **314**, 1757 (2006)



- 'Camelback' van Hove singularity is absent in BHZ model

NANO LETTERS

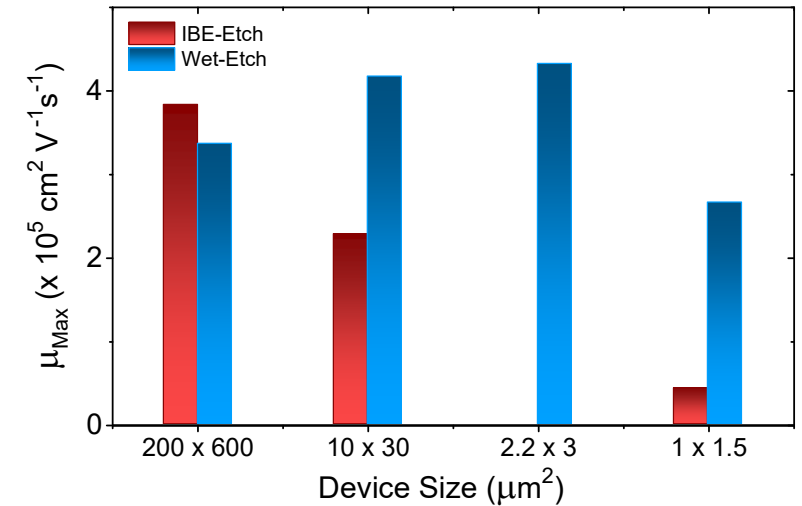
Cite This: *Nano Lett.* 2018, 18, 4831–4836

Letter

pubs.acs.org/NanoLett

High Mobility HgTe Microstructures for Quantum Spin Hall Studies

- Wet etching of nanostructures to avoid sample damage

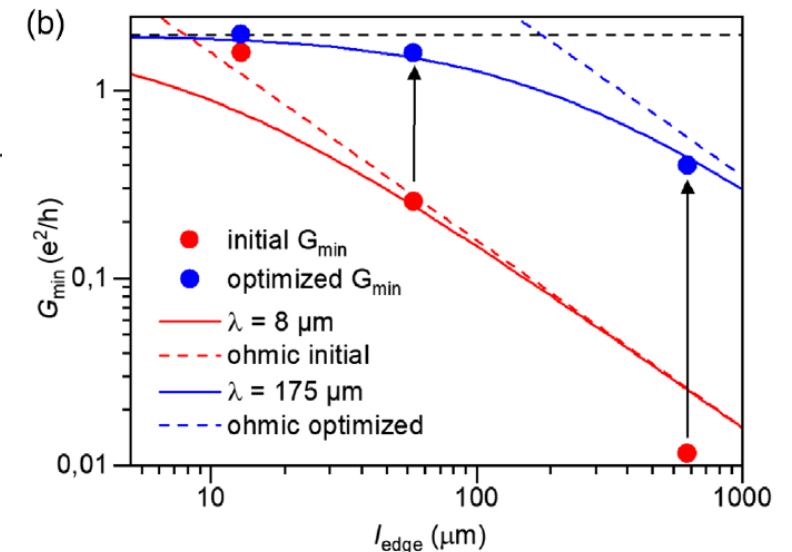


PHYSICAL REVIEW LETTERS **123**, 047701 (2019)

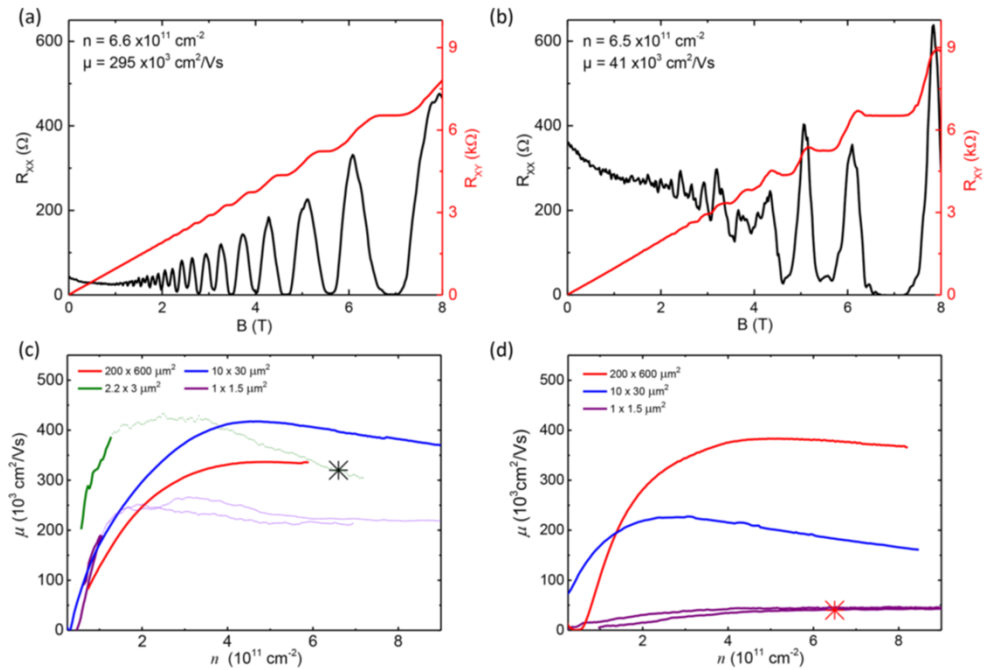
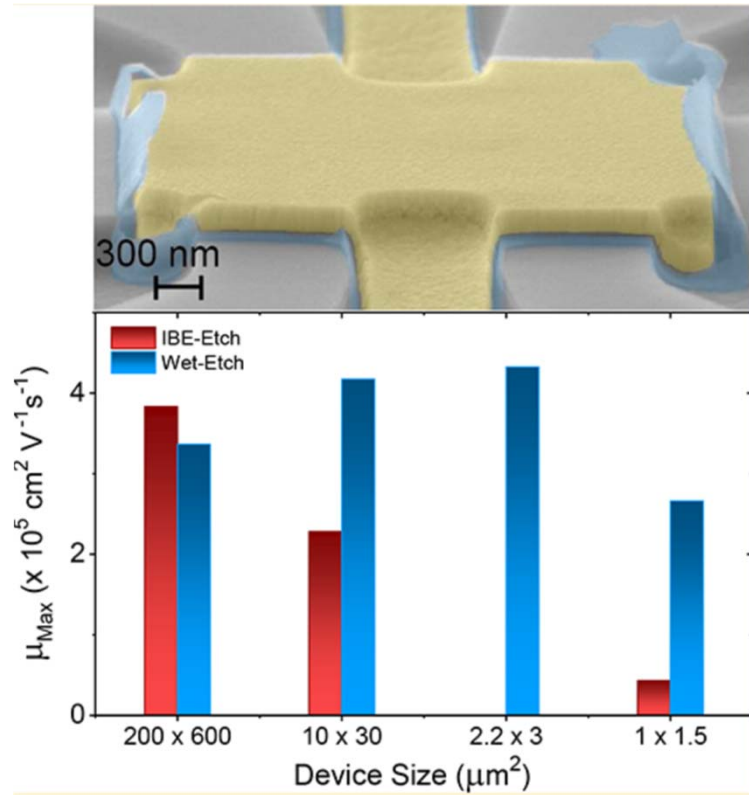
Editors' Suggestion

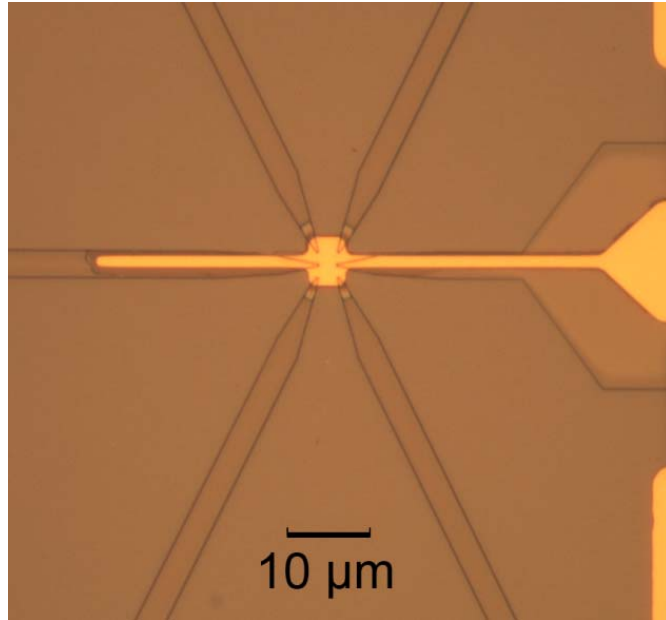
Approaching Quantization in Macroscopic Quantum Spin Hall Devices through Gate Training

- Gate training reduces puddle disorder
- Increases scattering length to ca. 100 μm

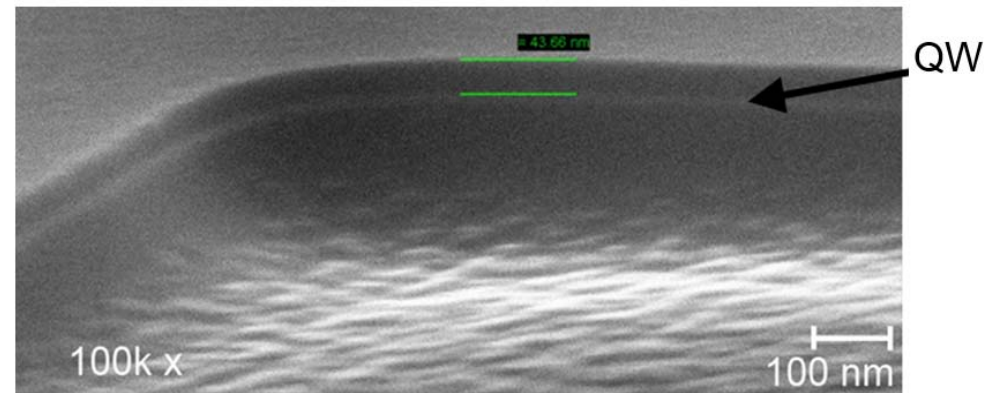
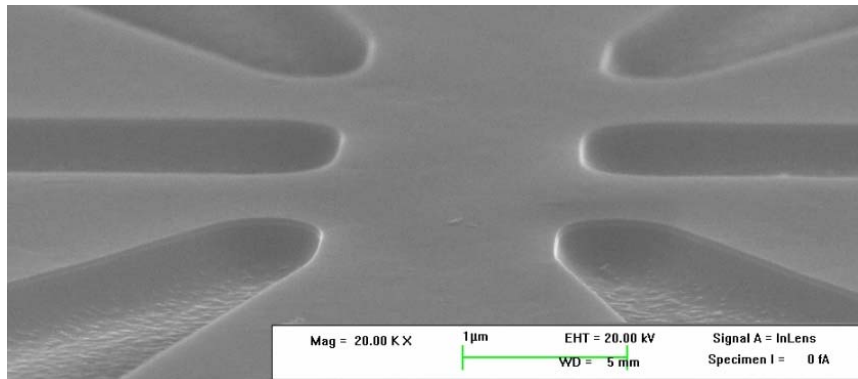
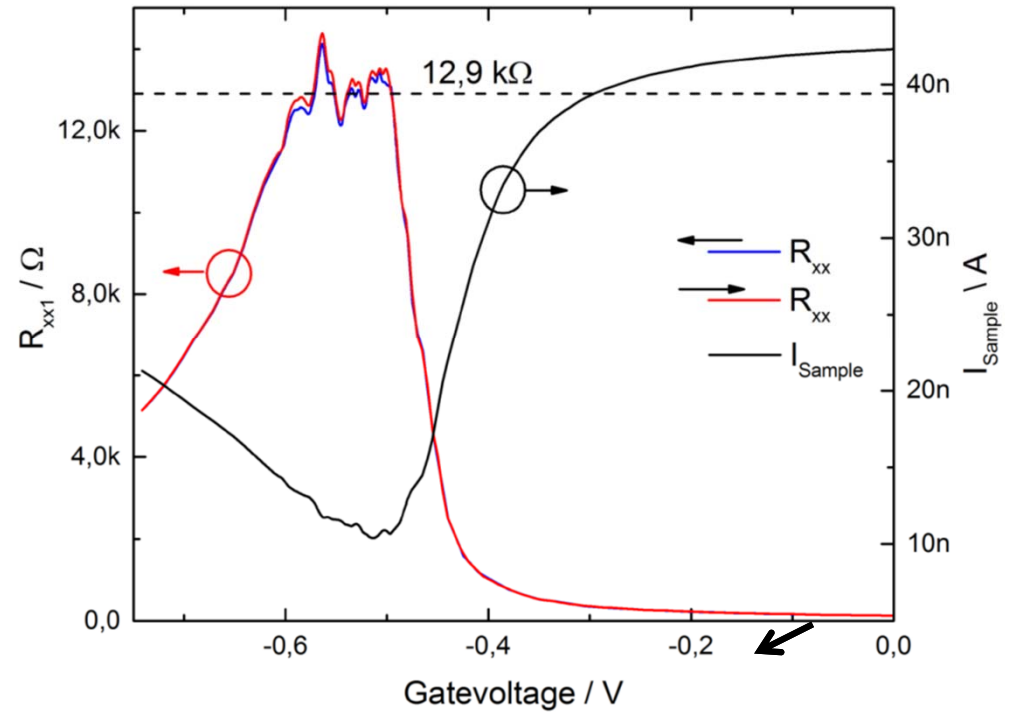


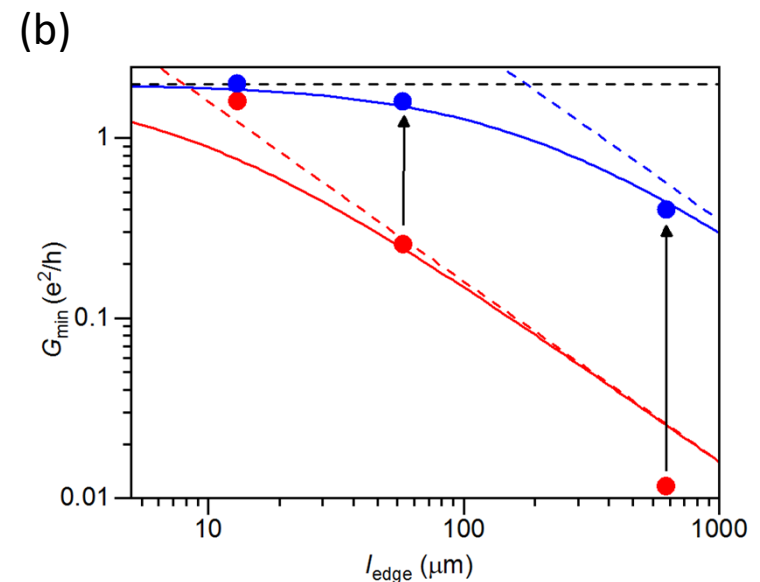
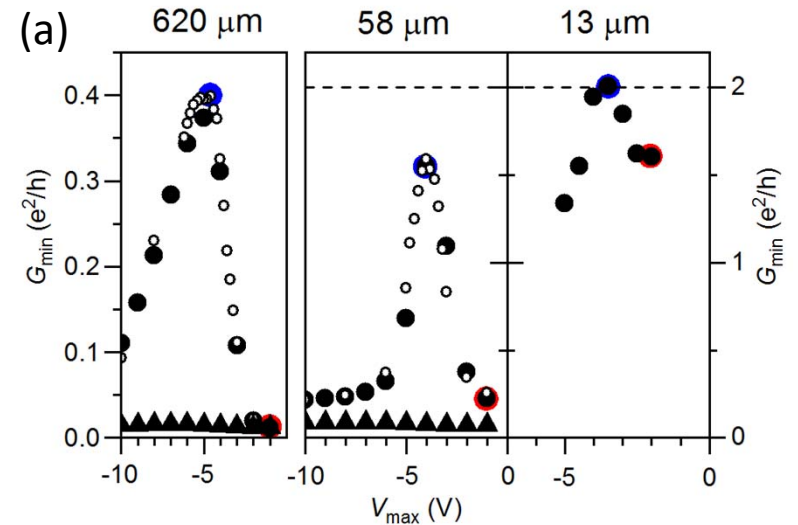
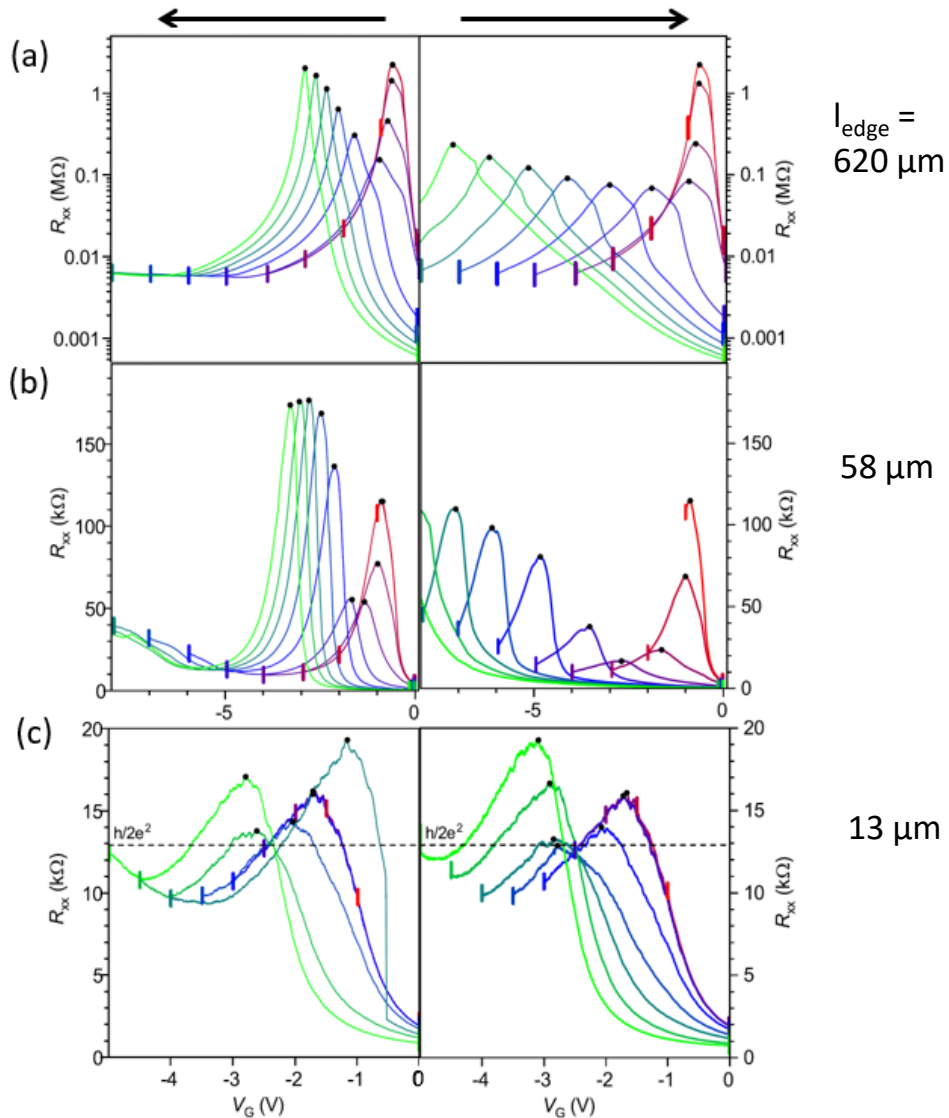
Wet etched micron-sized hall bars show strongly improved transport properties; better mobilities and better quantum Hall effect (homogeneity)





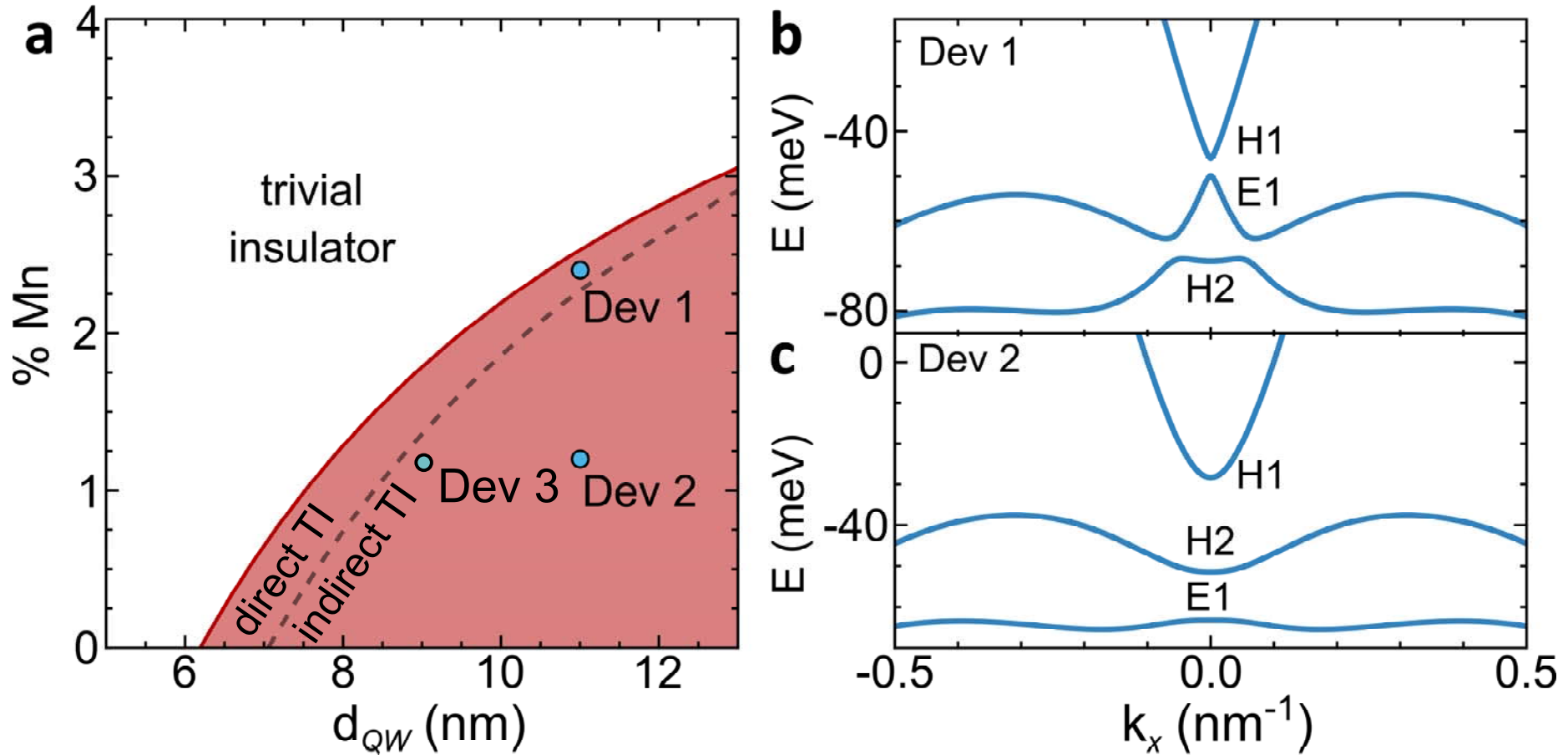
K. Bendias et al., Nano Lett. 10.1021, 2018





- The Mn atoms substitute Hg atoms isoelectrically: dilute magnetic II-VI semiconductor
- No change in carrier concentration; no degradation of device quality and no ferromagnetism, bandstructure influence is similar to other IIs
- Chemical composition: $\text{Hg}_{1-x}\text{Mn}_x\text{Te}$; x is in the range 0.01 – 0.025
- For the above concentration of Mn atoms, (Hg,Mn)Te QWs are paramagnetic; the magnetization is zero in the absence of an external magnetic field
- Giant Zeeman effect: at finite B, the magnetization can be calculated as $\langle m \rangle = -S_0 \frac{\vec{B}}{B} B_{5/2} \left(\frac{5 g_{\text{Mn}} \mu_B B T}{2 k_B (T + T_0)} \right)$
- g-factor enhanced through this magnetization (follows same Brillouin function.)
- Typical n density $\sim 10^{11} - 10^{12} \text{ cm}^{-2}$, typical mobility $\sim 2 \times 10^5 \text{ cm}^{-2} \text{ V}^{-1} \text{ s}^{-1}$

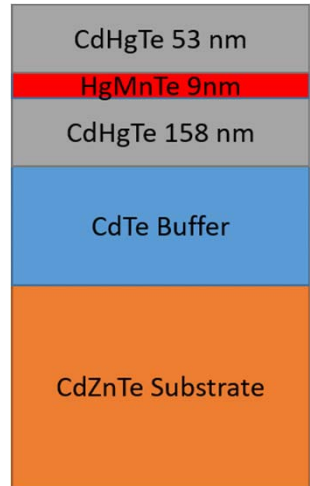
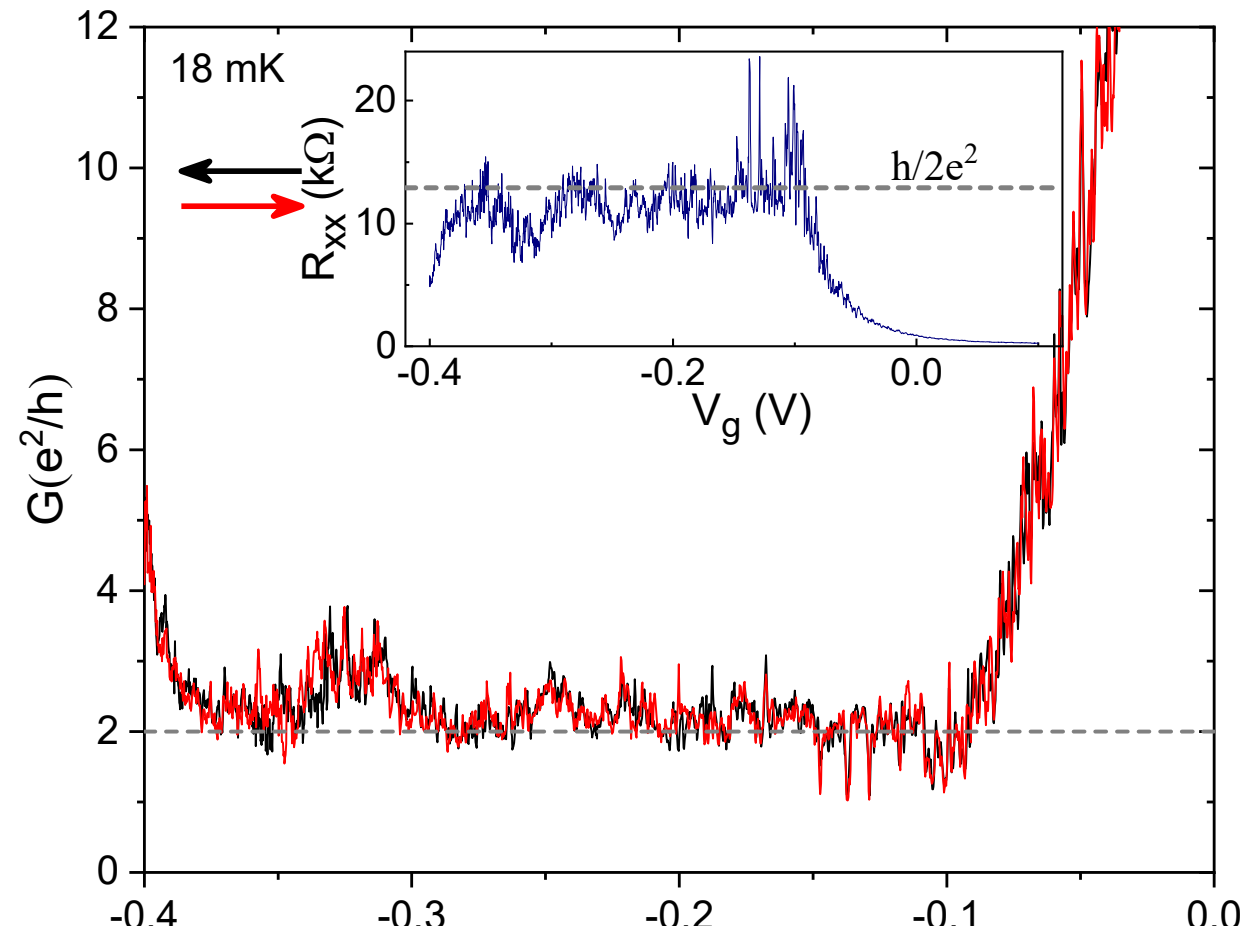
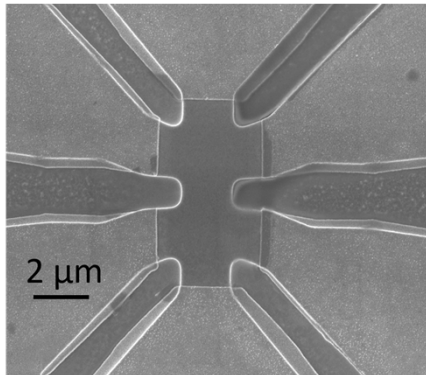
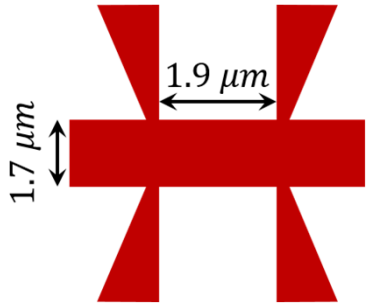
- Can we observe the quantized conductance when we add magnetic impurities?
- Effect of magnetic field on the edge channels – Do the edge channels survive the breakdown of time reversal symmetry
- Effect of the van Hove singularity in the valence band?



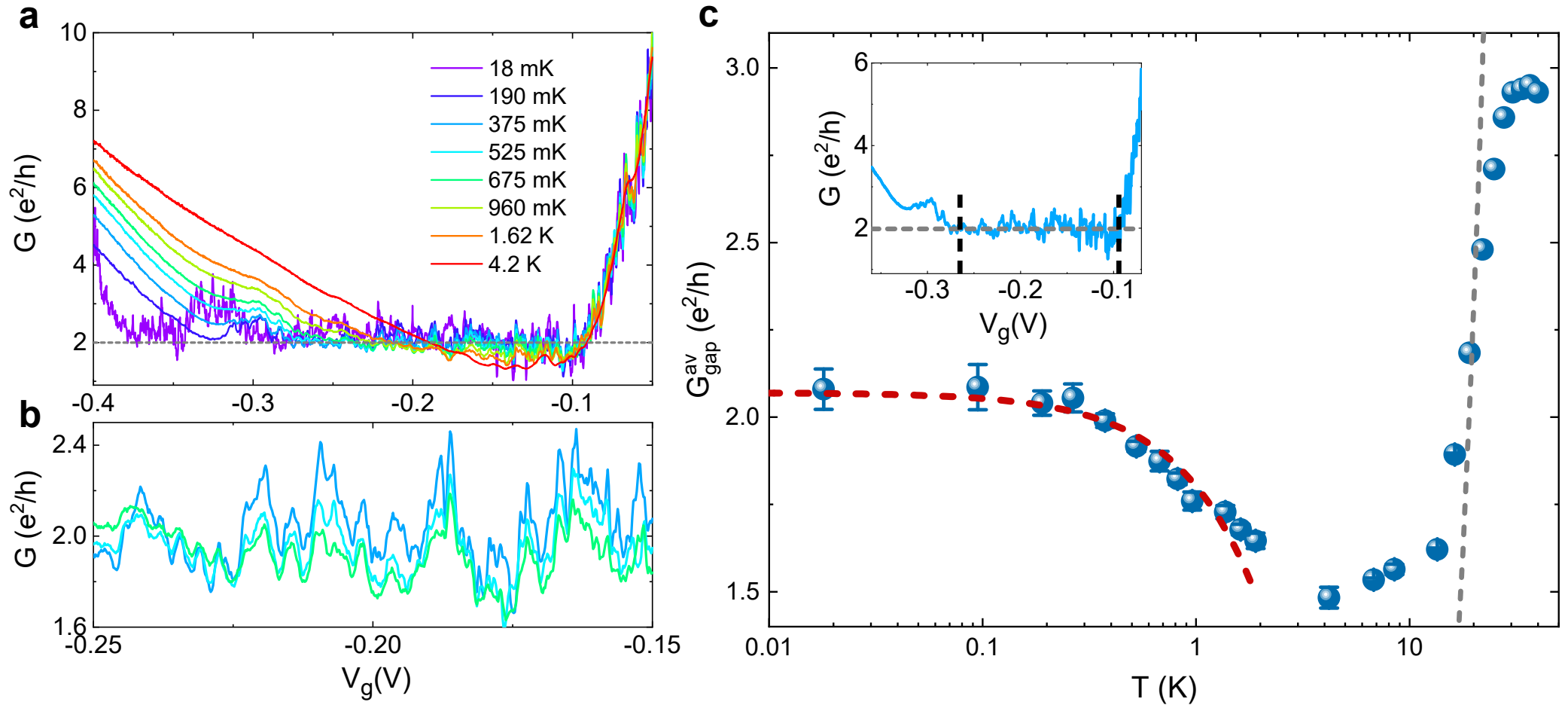
Breaking Time Reversal Symmetry in a Topological Insulator

- Will adding magnetic impurities destroy the quantum spin Hall effect ?
- Very different predictions about fate of the quantum spin Hall effect in the presence of magnetic impurities (can cause spin-flip scattering and break local time reversal symmetry):
 - No effect (Tanaka et al., PRL 2011)
 - Anderson localization (Altshuler et al., PRL 2013)
 - Kondo screening (Maciejko et al., PRL 2009)

Dev 3: 9 nm QW, 1.2% Mn

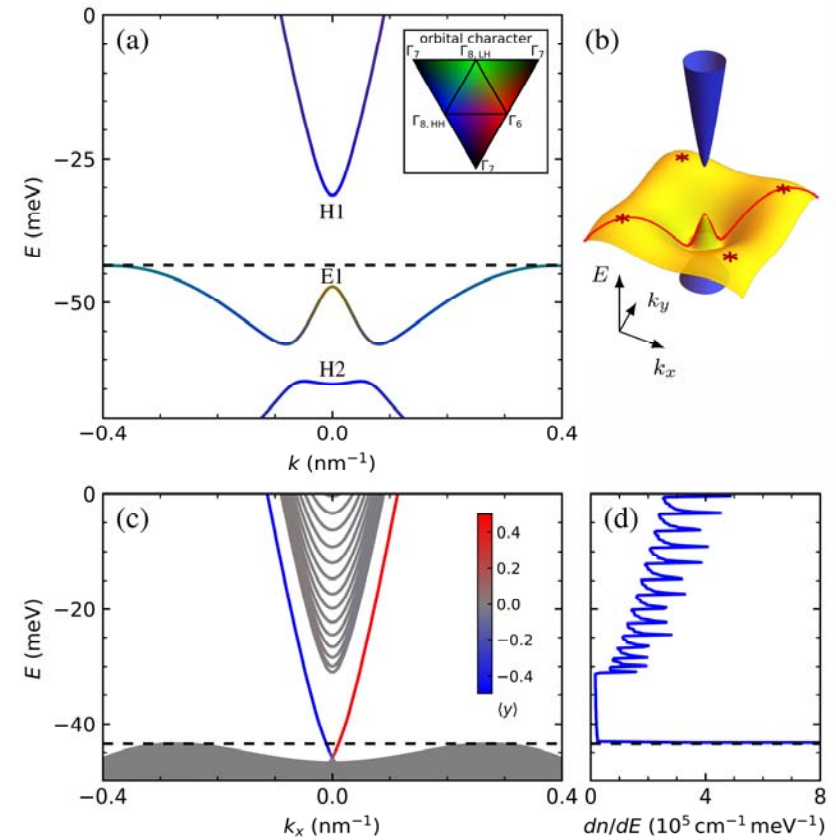
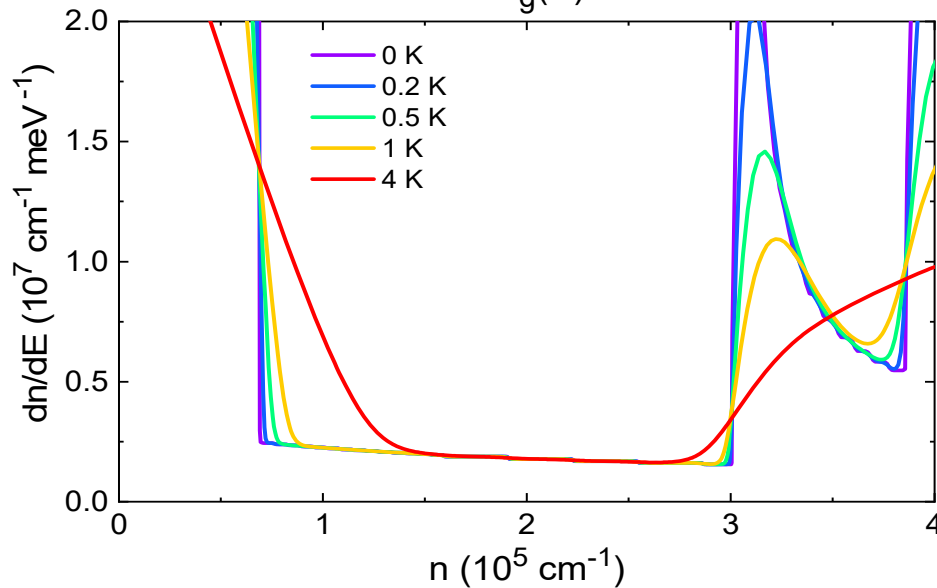
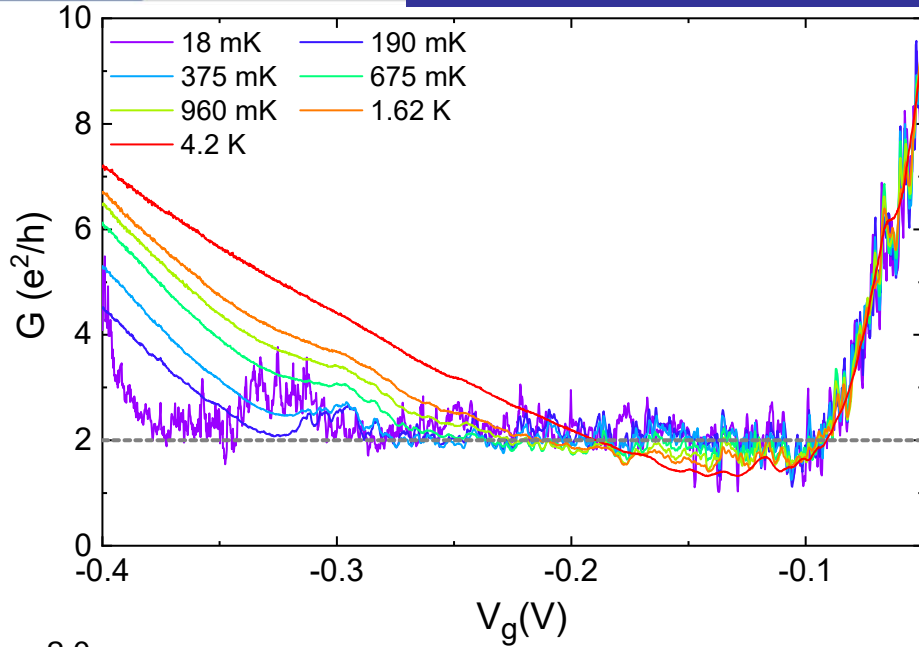


- After gate training, we observe clear conductance quantization of the quantum spin Hall effect in the presence of magnetic impurities.
- Very long plateau due to camelback

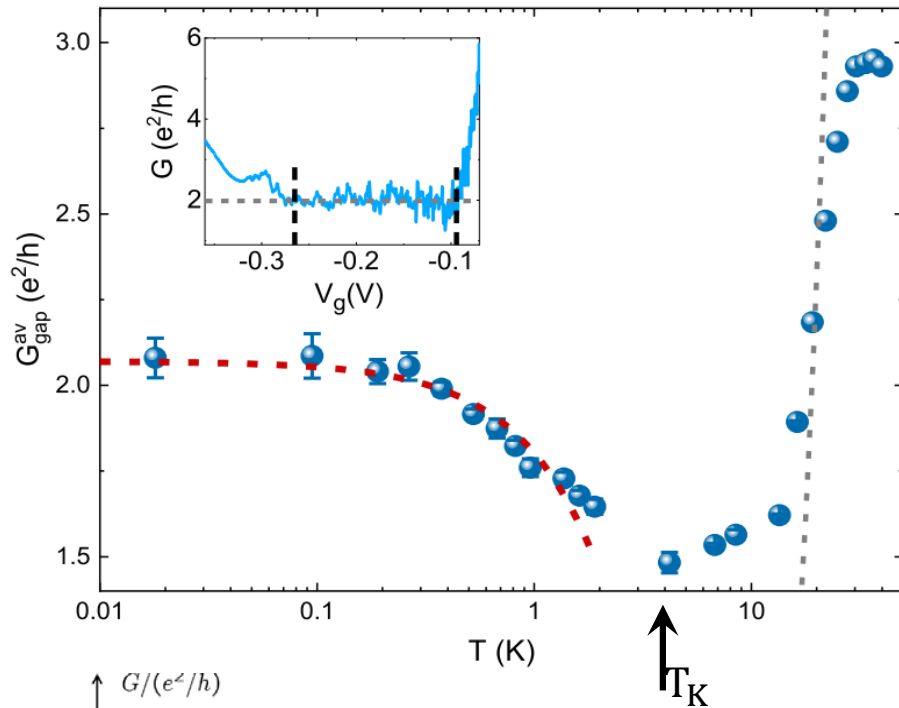


Low temperature behavior suggests Kondo screening of the magnetic impurity at low temperature.

Thermal activation of plateau width: Camelback in valence band



Wouter Beugeling



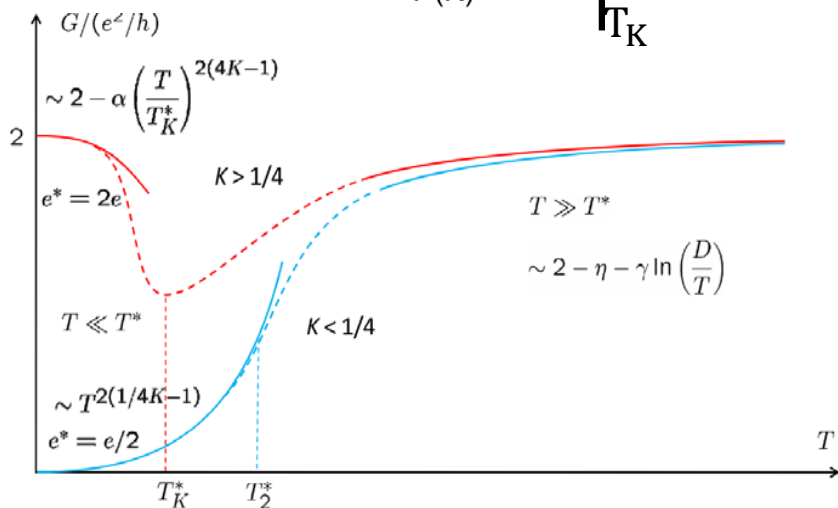
Comparison with theory by Maciejko *et. al.*, *PRL* **102**, 256803 (2009).

Interaction parameter

$$K = \left[1 + \frac{2}{\pi} \frac{e^2}{\epsilon_0 \epsilon_r \hbar v_F} \ln \left(\frac{7.1d}{\xi + 0.8w} \right) \right]^{-1/2} \sim 0.5.$$

Assumes isotropic scattering.

High temperature activation simply results from thermal across-gap excitation

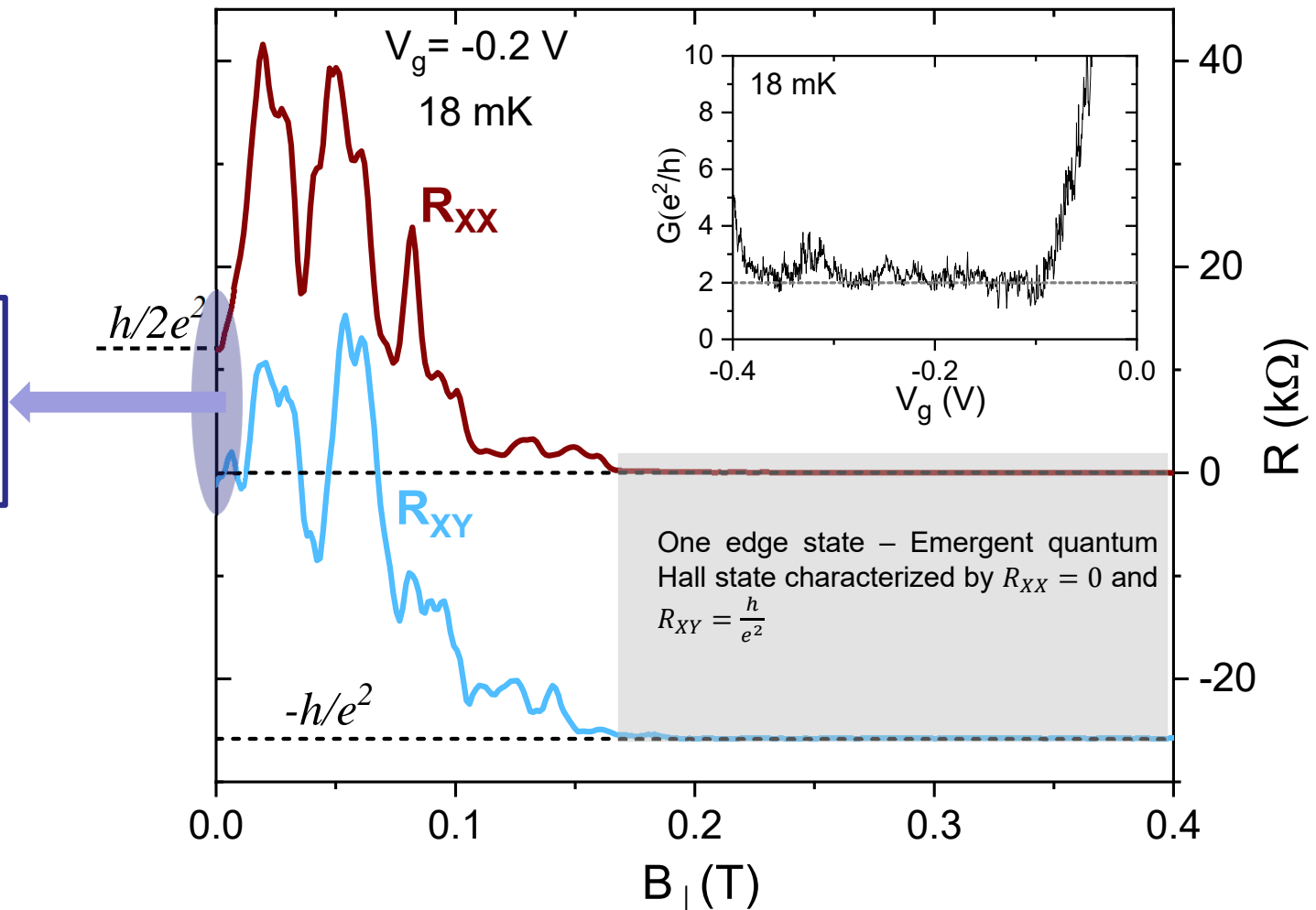


Breaking Time Reversal Symmetry in a Topological Insulator

- Adding magnetic impurities does not destroy the quantum spin Hall effect
- What will a magnetic field do, i.e. global breaking of time reversal symmetry?

Dev 3: 9 nm QW, 1.2% Mn

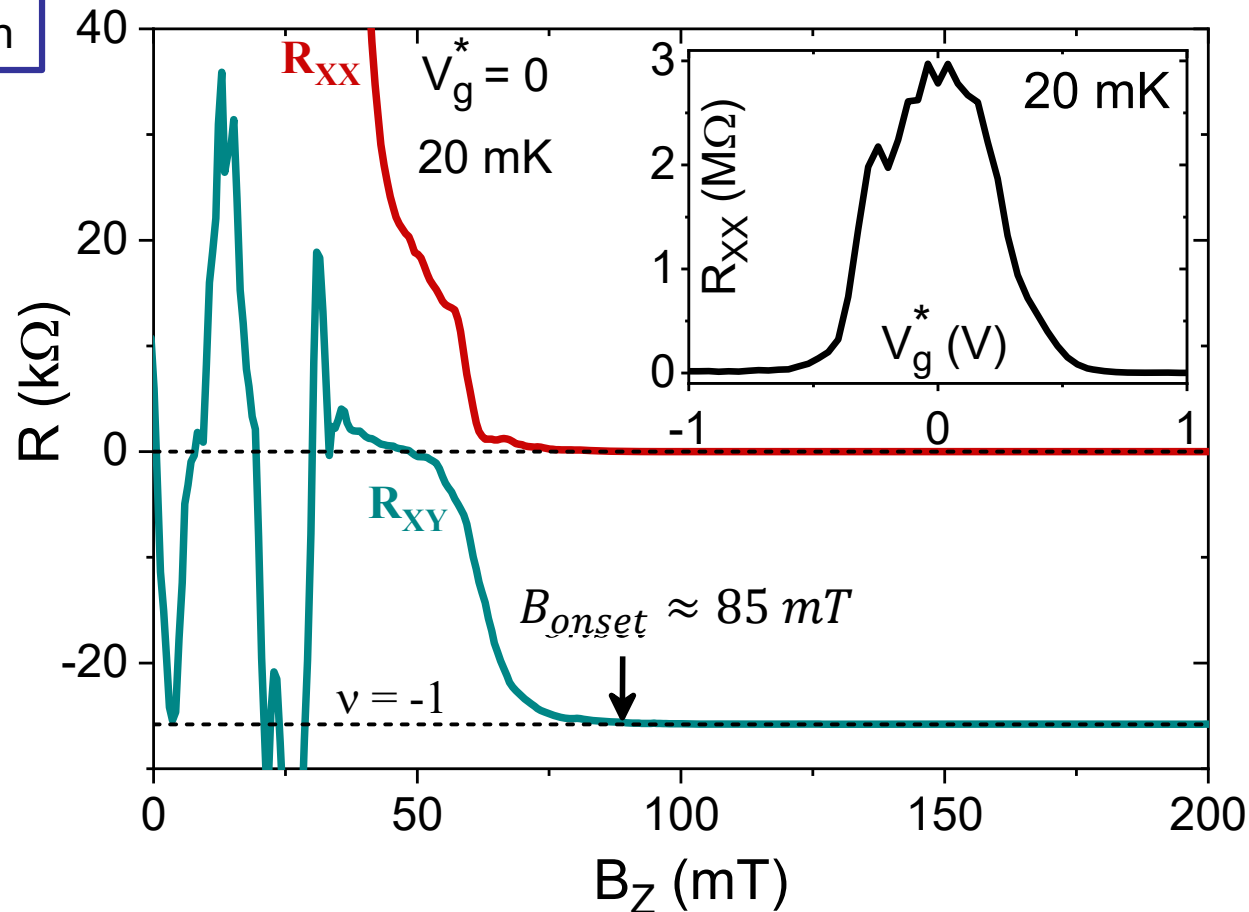
Quantum spin Hall effect at $B = 0\text{T}$ characterized by $R_{XX} = \frac{h}{2e^2}$ and $R_{XY} = 0$



- Onset of $\nu = -1$ plateau at **unexpectedly low** perpendicular magnetic field

Emergence of QH effect from QSH edge states

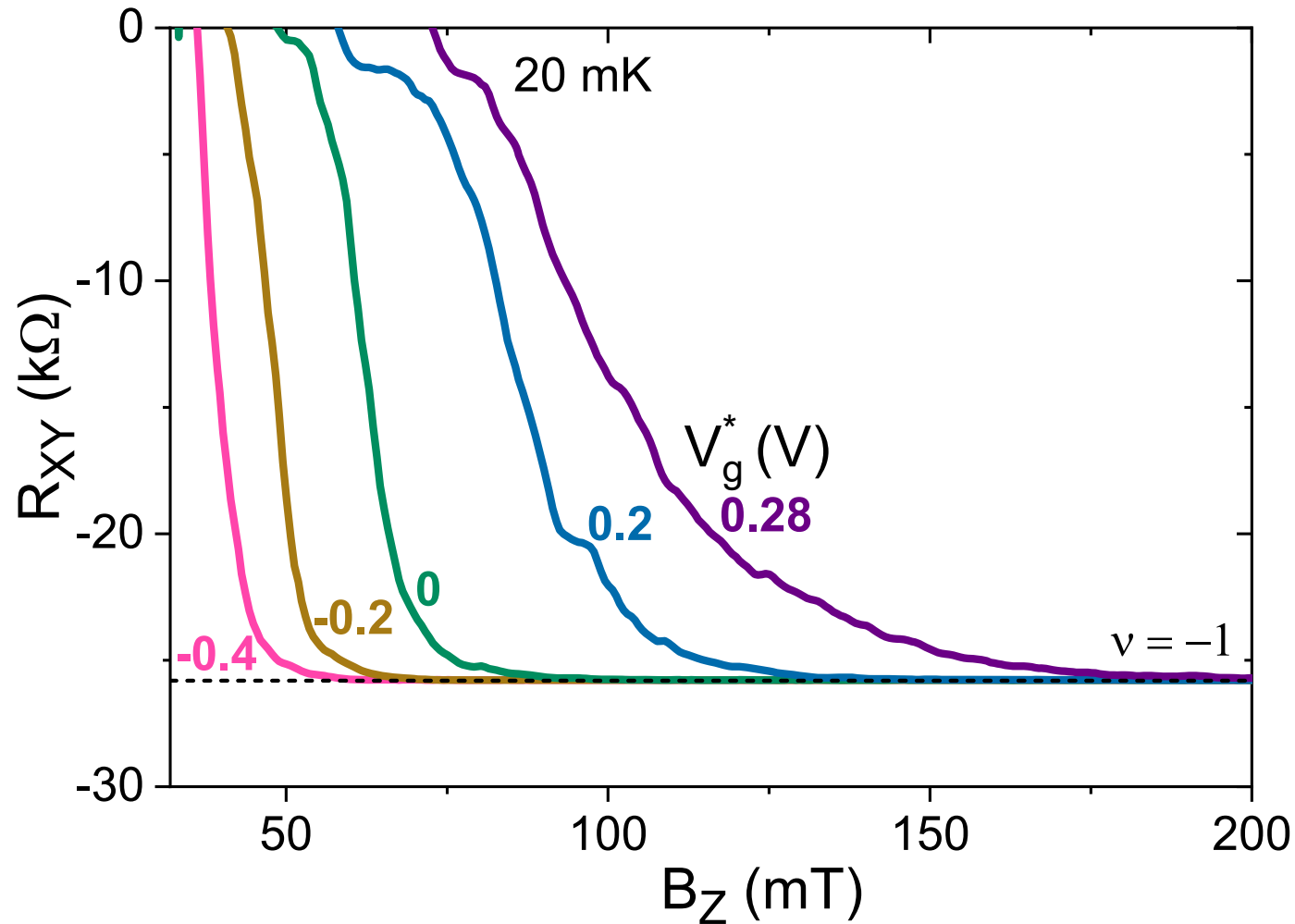
Dev 1: 11 nm QW, 2.4% Mn

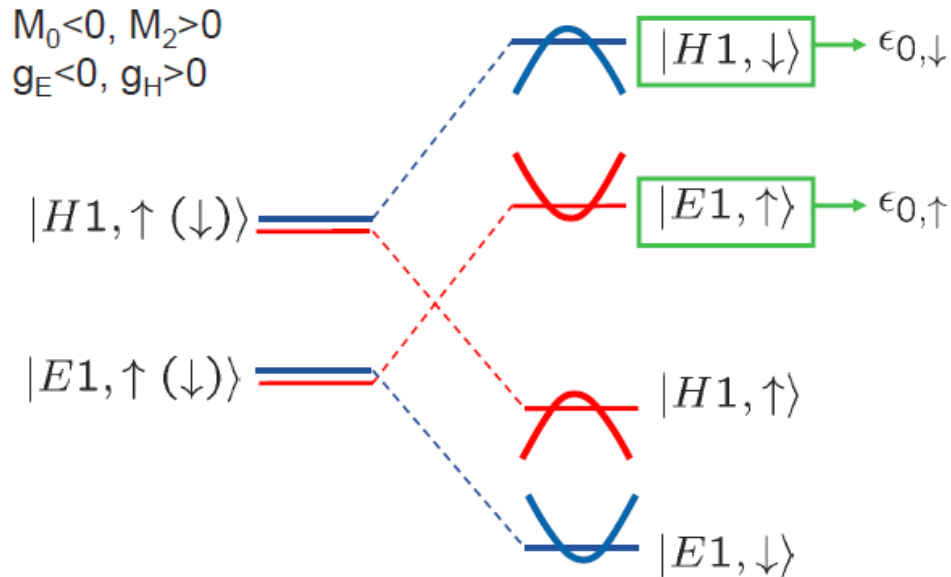


- Macroscopic Hall bar ($600 \times 200 \mu\text{m}^2$), 11 nm (Hg,Mn)Te QW with 2.4% Mn
- Not quantized at zero field because of large device dimensions
- More suited to explore various aspects of QHE in (Hg,Mn)Te due to cleaner Hall signal in large device
- Onset of $\nu = -1$ plateau at unexpectedly low perpendicular magnetic field

Dev 1: 11 nm QW, 2.4% Mn

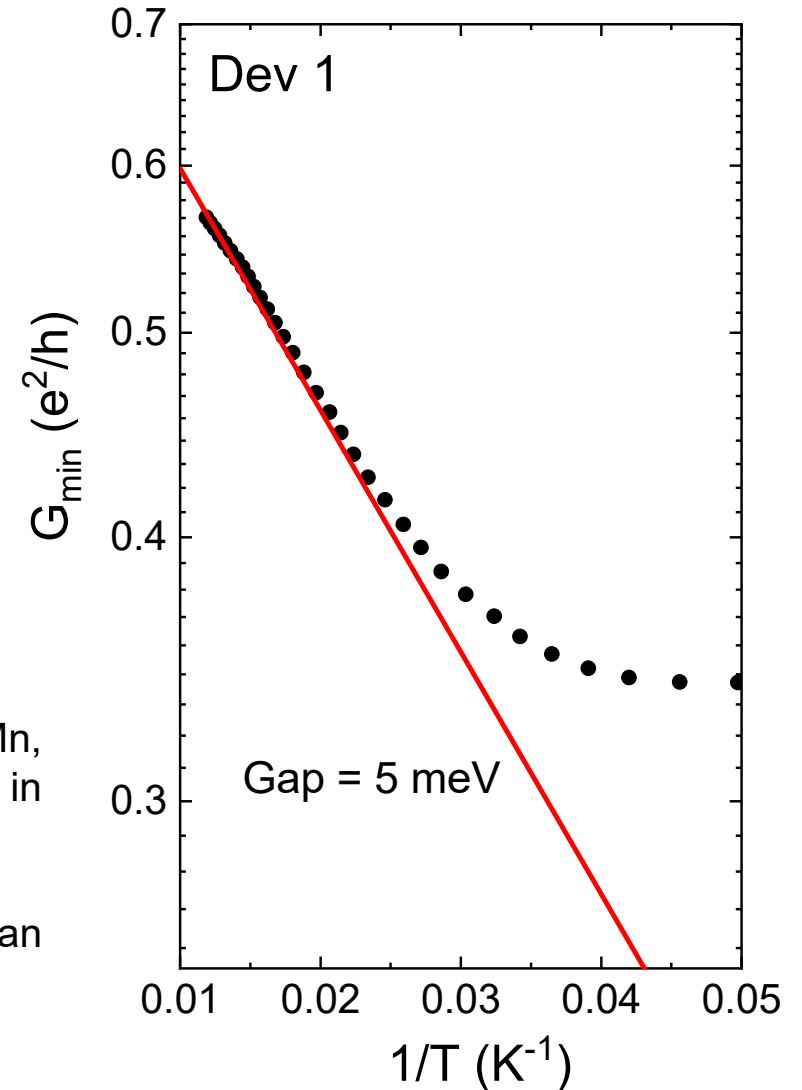
- Influence of gate voltage on $\nu = -1$ plateau

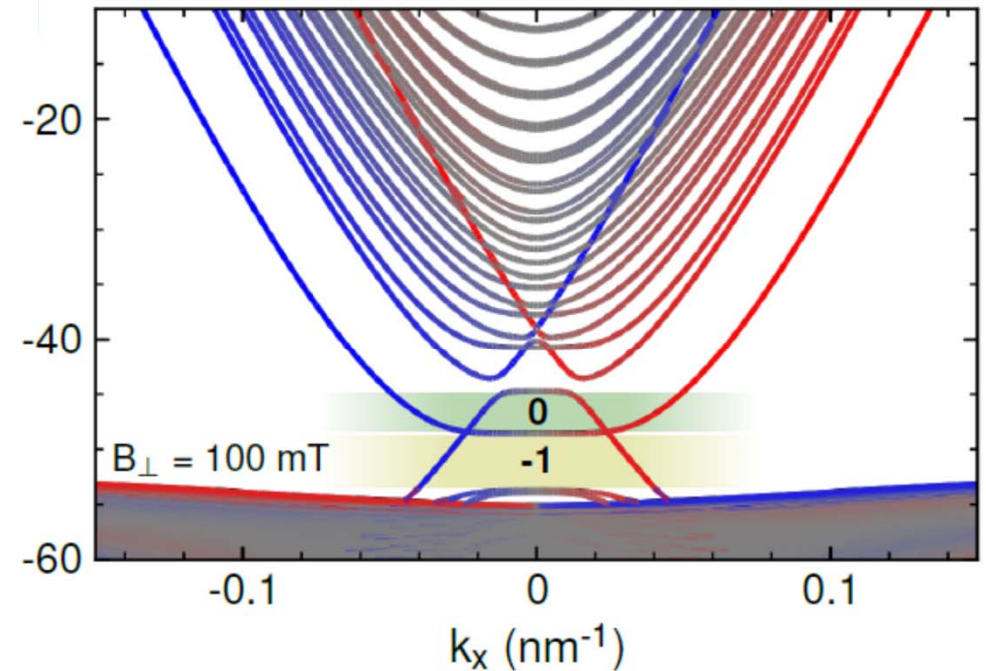
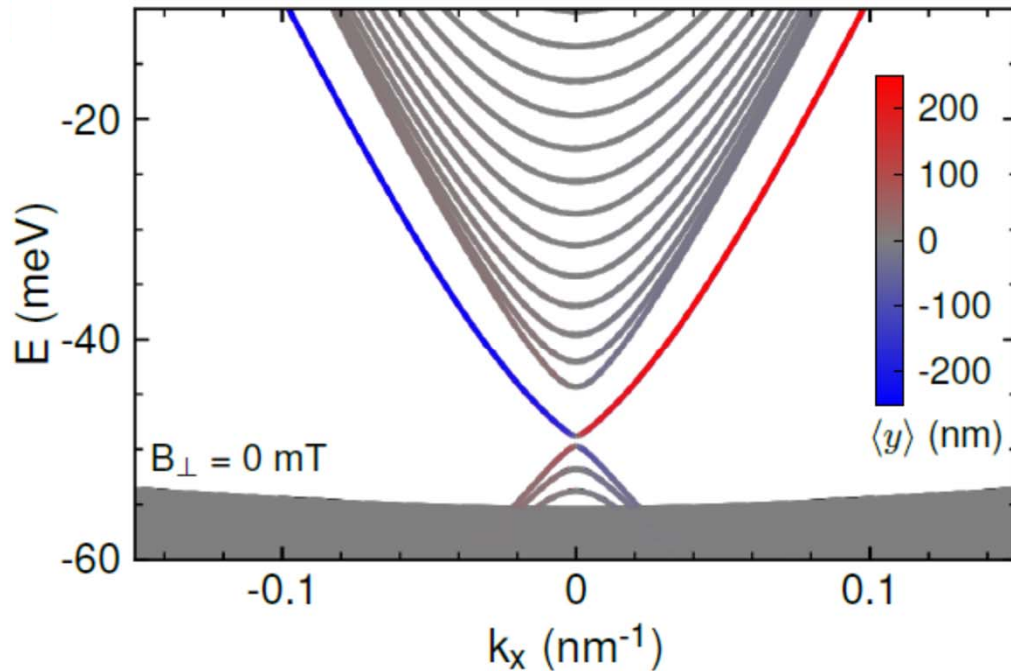




Phys. Rev. Lett. **101**, 146802 (2008)

- From C. X. Liu et al., PRL 101, 146802 (2008), for 2% Mn, magnetization $\langle S \rangle > 0.5$ need to close the gap for realizing the QAHE in HgMnTe
- Here, the onset occurs at $B_{\perp} \approx 0.1$ T, corresponding to $\langle S \rangle \approx 0.15$; can close a gap of 1 meV
- Different mechanism at play!! \Rightarrow Back to k.p calculations





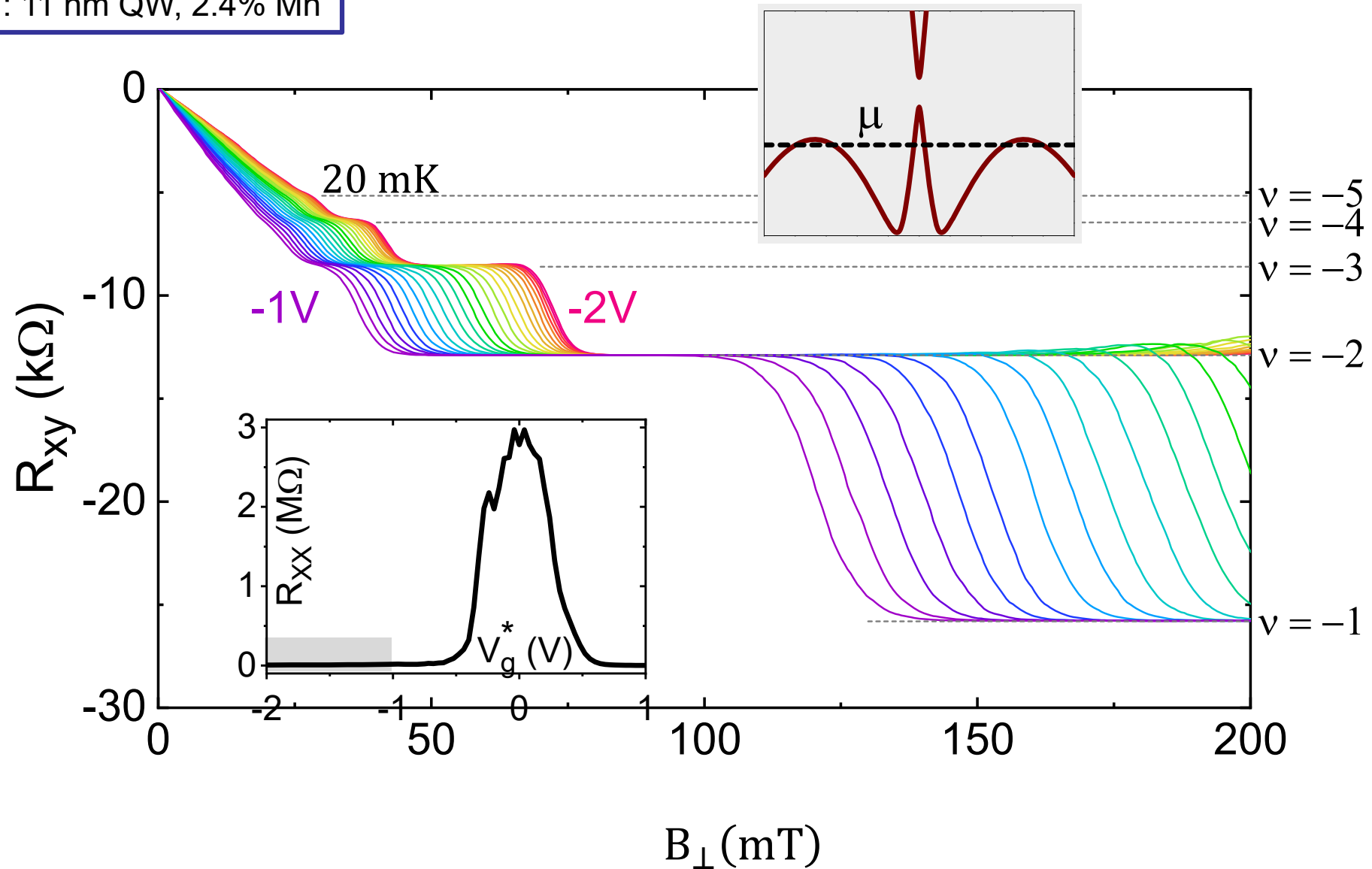
Calculations: W. Beugeling

- At zero field, Dirac point is just above camel's back.
- At finite fields, one spin state shifts down, leaves the topological gap and hybridizes with large dos at camel's back.
- The other shifts up and remains unhybridized with cb bulk states (different k value)
- Emergent $\nu = -1$ QH state in the LL gap

One quantum spin Hall edge channel survives the breakdown of time reversal symmetry

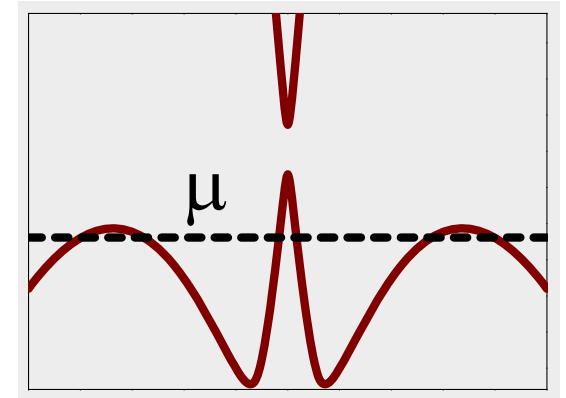
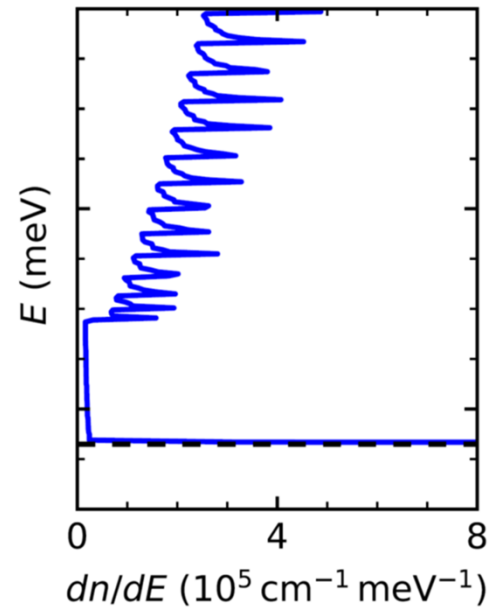
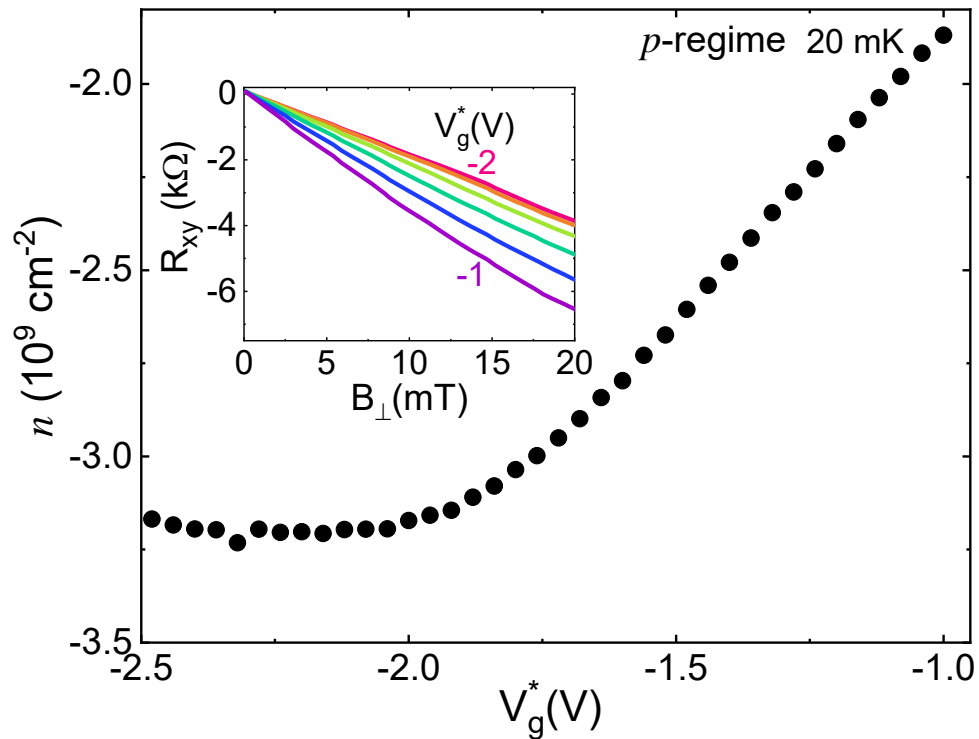
Next, we tune the Fermi level into the bulk valence band

Dev 1: 11 nm QW, 2.4% Mn



Dev 1: 11 nm QW, 2.4% Mn

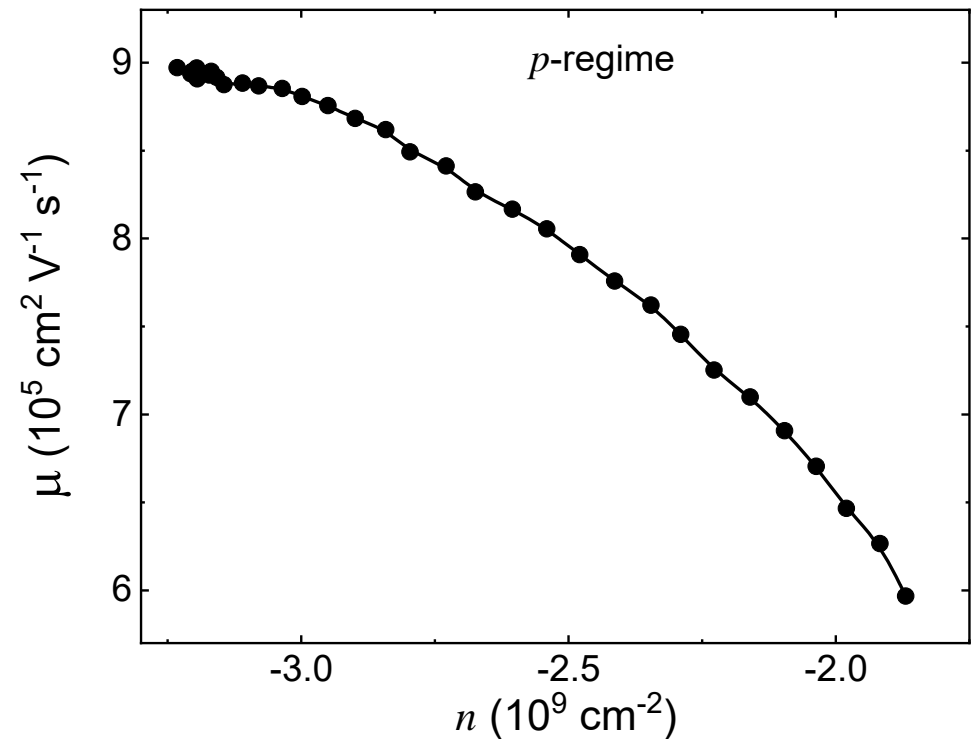
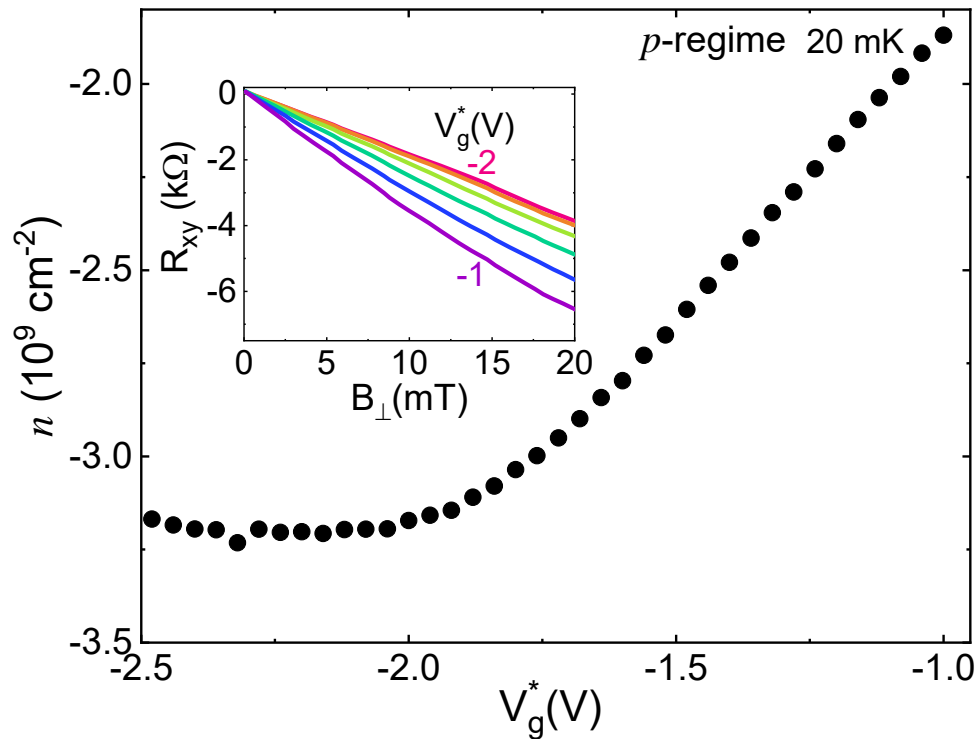
Expected carrier density, from the gate efficiency - $5 \times 10^{11} \text{ cm}^{-2}$



Localized carriers at the *camelback*

Dev 1: 11 nm QW, 2.4% Mn

Expected carrier density, from the gate efficiency - $5 \times 10^{11} \text{ cm}^{-2}$



Localized carriers at the *camelback*

Extremely low density two dimensional system with *extremely* high mobility

Two-dimensional massless electrons in an inverted contact

JETP Lett. **42**, 178 (1985)

B. A. Volkov and O. A. Pankratov

P. N. Lebedev Physics Institute, Academy of Sciences of the USSR

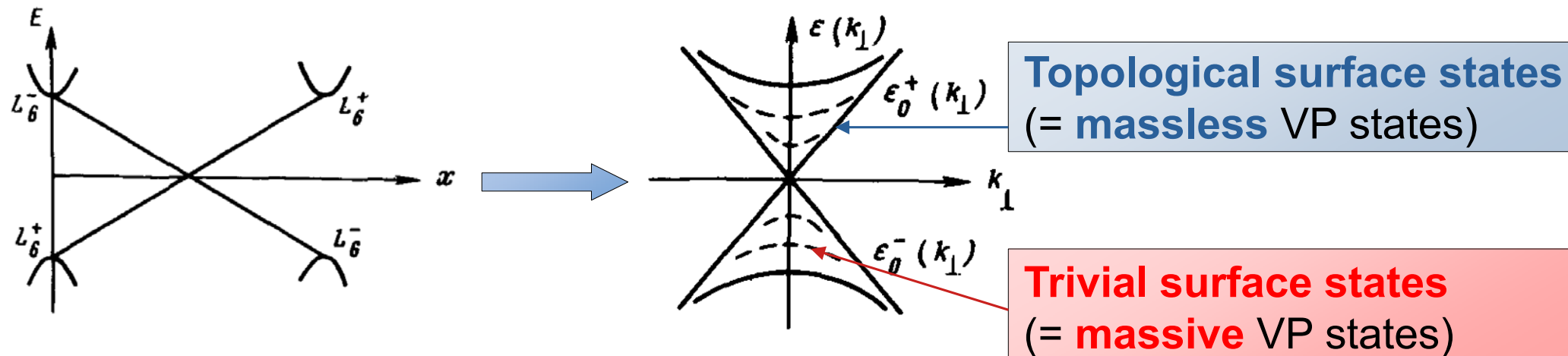


FIG. 2. Energy spectrum of the inverted contact. Solid curves—The Dirac (band) state and the Weyl state; dashed curves—additional branches which arise when the contact thickness is $l > l_0$.

In hindsight, topological insulators were almost predicted in the mid-1980s and directly connected with the parity anomaly!

$$\begin{aligned}\sigma_{xy} &= -\frac{1}{2} \frac{e^2}{h} \sum_i \chi_i \operatorname{sgn}(m_i) \\ &= -\frac{1}{2} \frac{e^2}{h} [\operatorname{sgn}(m_1) - \operatorname{sgn}(m_2)]\end{aligned}$$

(for two Dirac fermions)

- G. W. Semenoff, Phys. Rev. Lett. **53**, 2449 (1984).
- B. A. Volkov and O. A. Pankratov, JETP Lett. **42**, 178 (1985).
- F. V. Kusmartsev and A. M. Tselik, JETP Lett. **42**, 257 (1985).
- E. Fradkin, E. Dagotto, and D. Boyanovsky, Phys. Rev. Lett. **57**, 2967 (1986).
- F. D. M. Haldane, Phys. Rev. Lett. **61**, 2015 (1988).

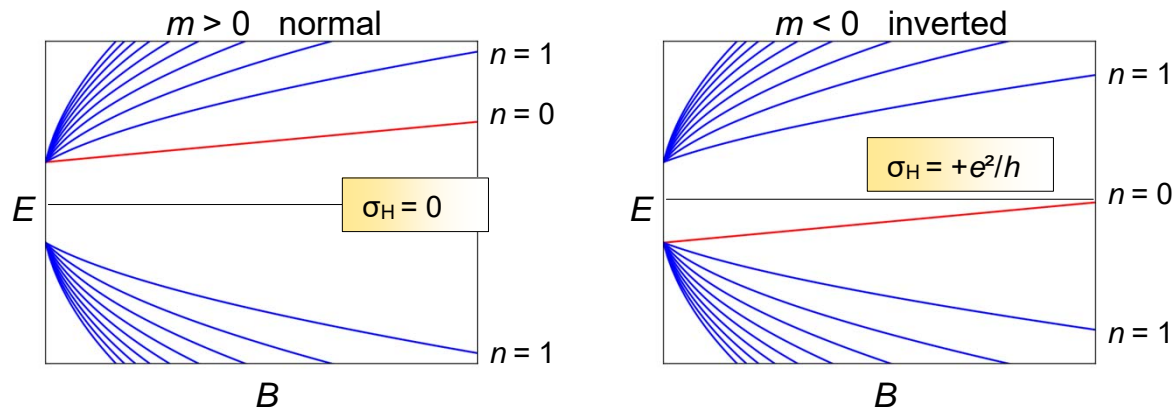
Model for a single Dirac electron: ($\approx 1/2$ BHZ model)

$$H = C\sigma_0 + m\sigma_z - \mathcal{A}(k_y\sigma_x - k_x\sigma_y) = \begin{pmatrix} C + m & -i\mathcal{A}k_- \\ i\mathcal{A}k_+ & C - m \end{pmatrix}$$

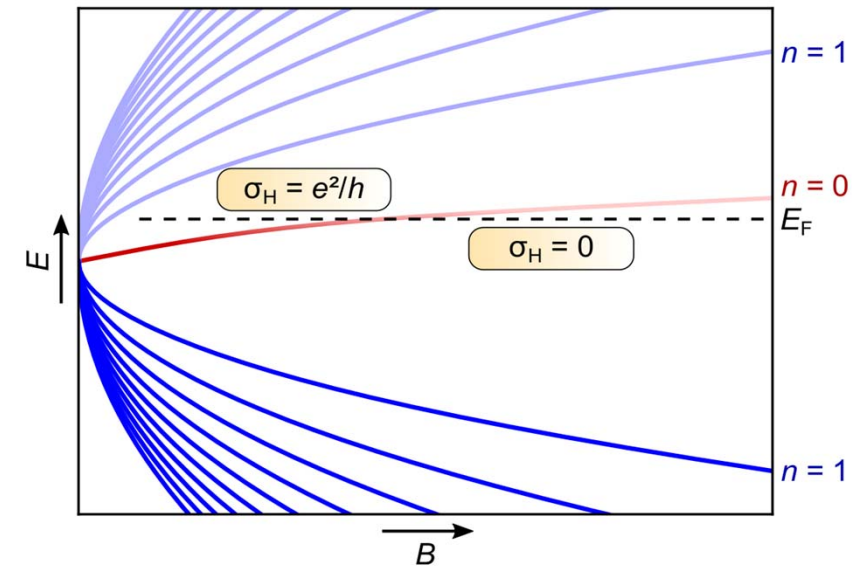
Dirac mass:
 $m > 0$ normal
 $m < 0$ inverted

parity anomaly
no gauge invt theory of
single parity invariant
Dirac particle in 2+1D

- G. W. Semenoff, Phys. Rev. Lett. **53**, 2449 (1984).
- E. Fradkin, E. Dagotto, and D. Boyanovsky,
Phys. Rev. Lett. **57**, 2967 (1986).
- F. D. M. Haldane, Phys. Rev. Lett. **61**, 2015 (1988).

Dirac electron in a magnetic field B 

There is only a single zero Landau level ($n = 0$)



Spectral asymmetry

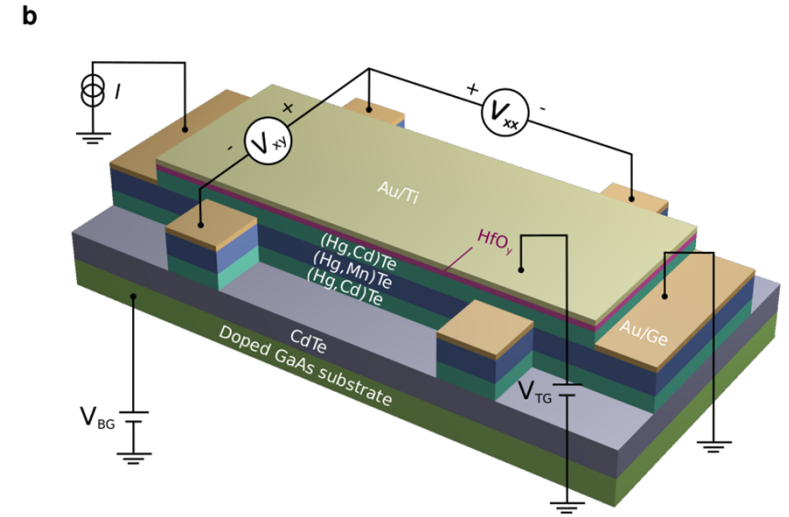
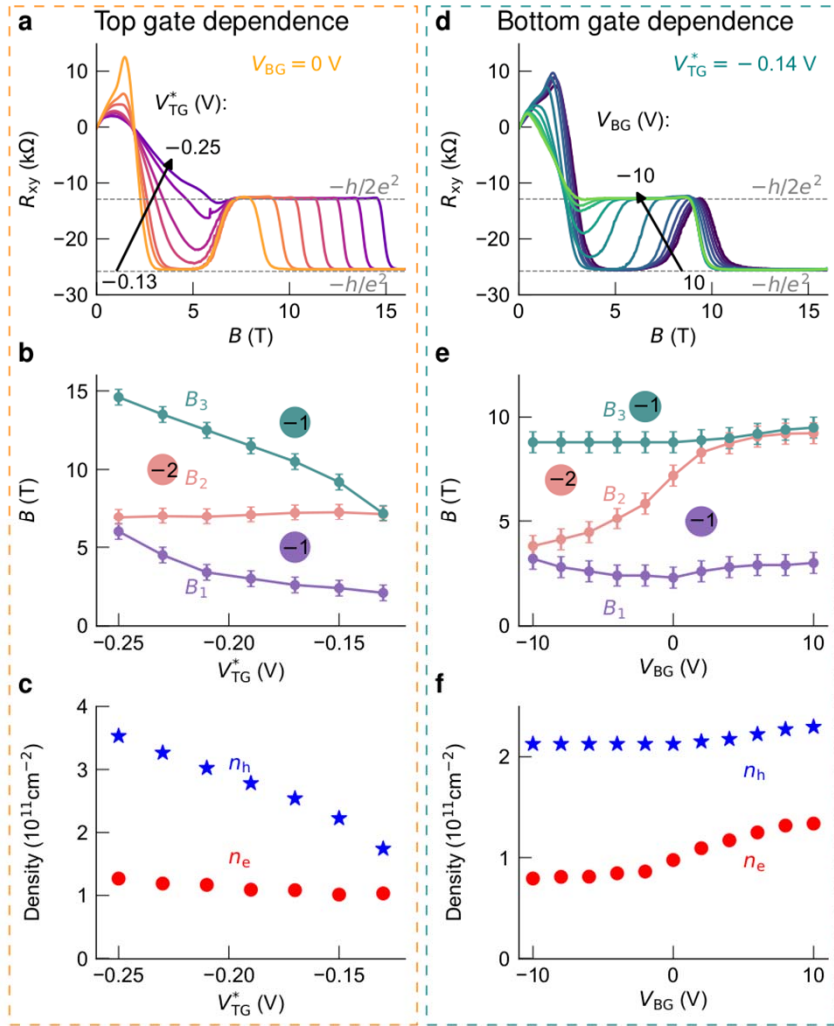
Normal band ordering

→ $\sigma_H = 0$

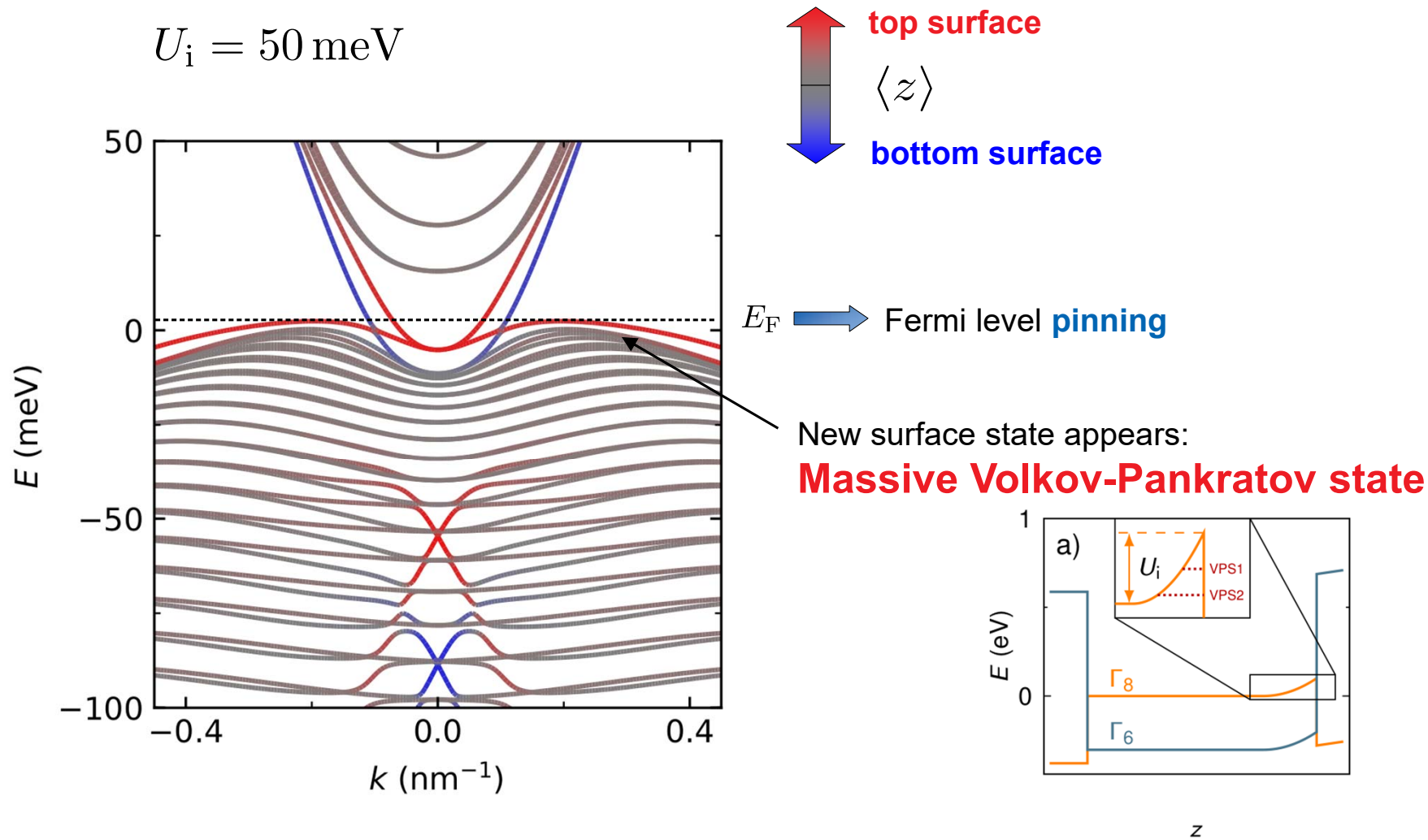
Inverted bands

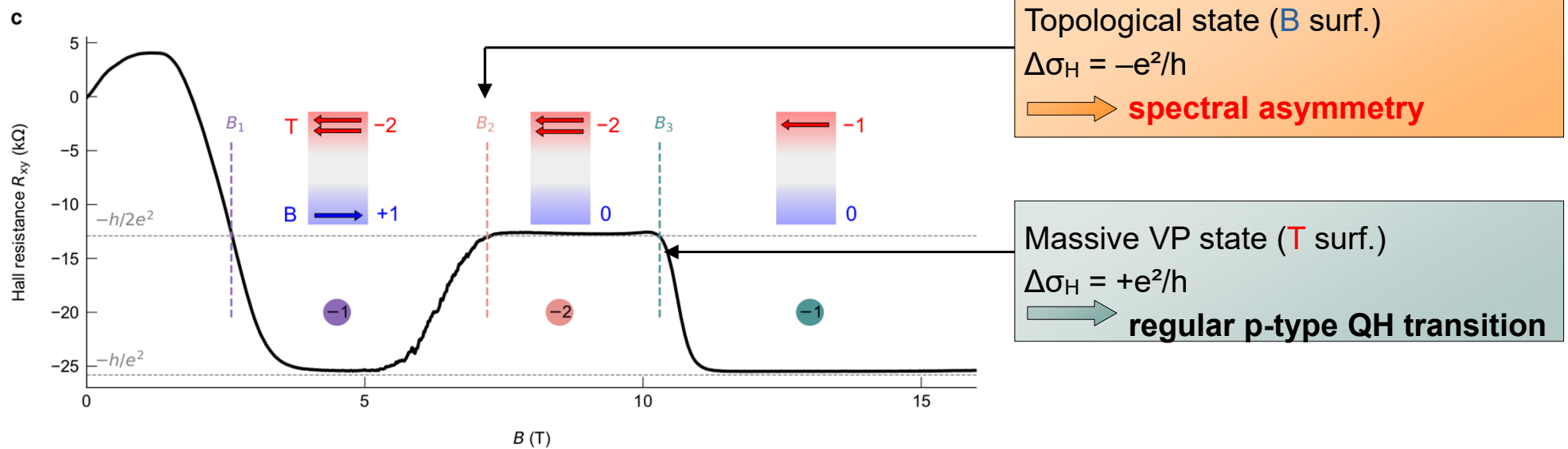
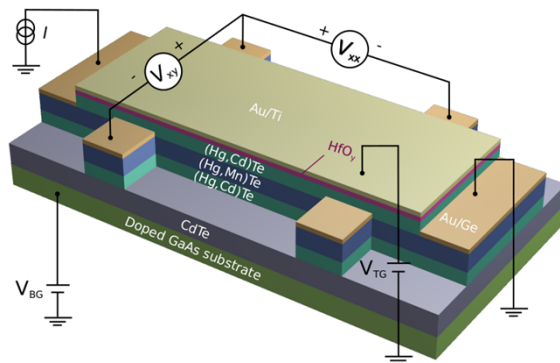
→ $\sigma_H = +e^2/h$

Magnetotransport!



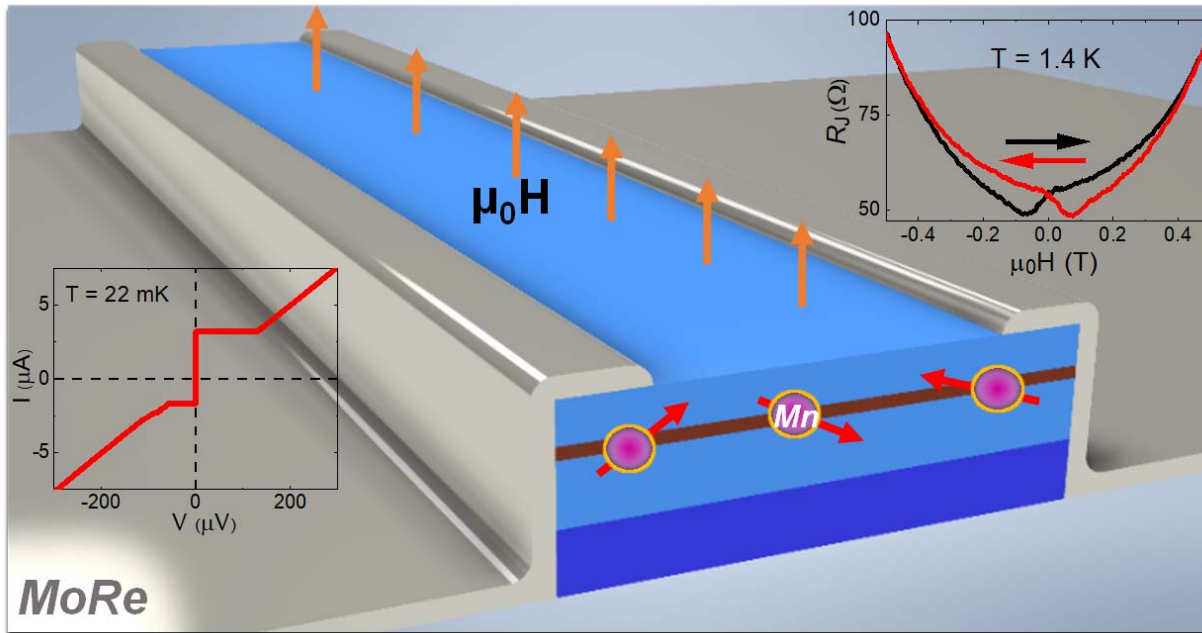
Lixian Wang, et al. (submitted)



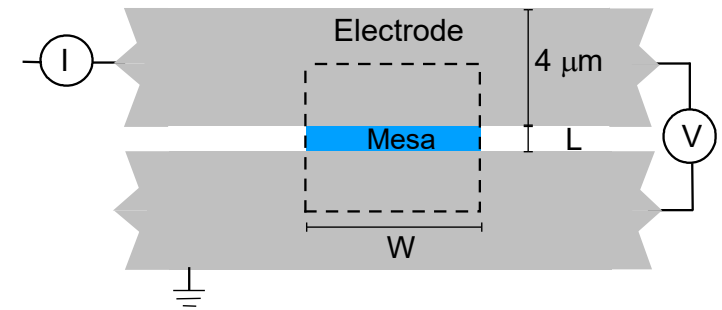
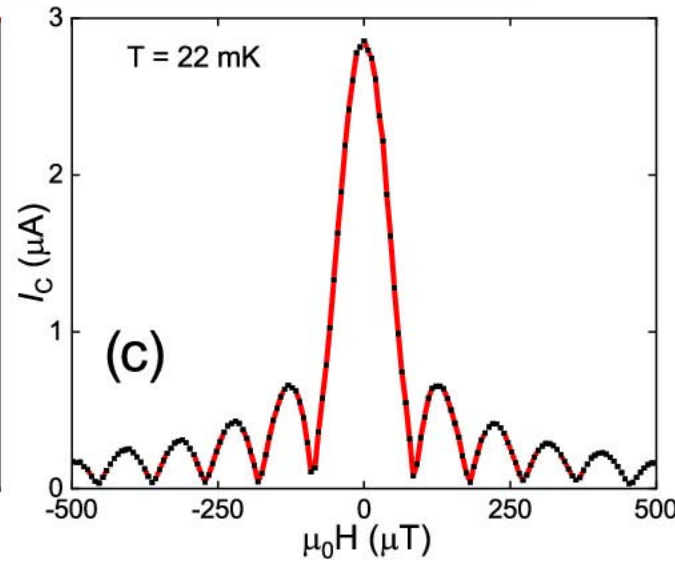
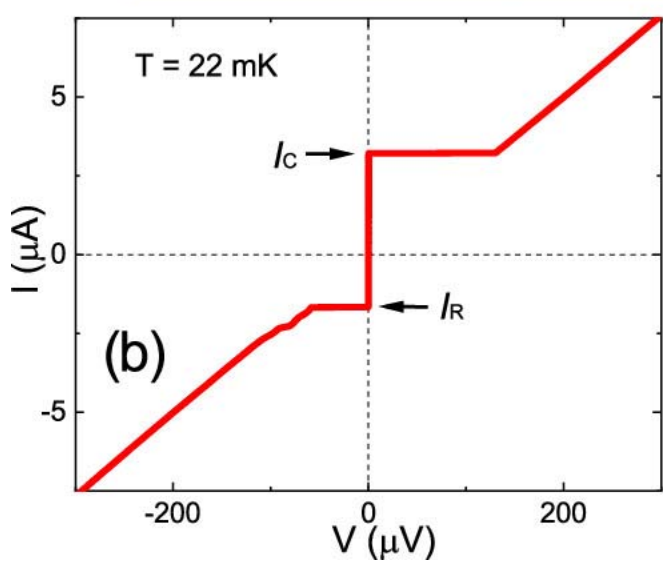
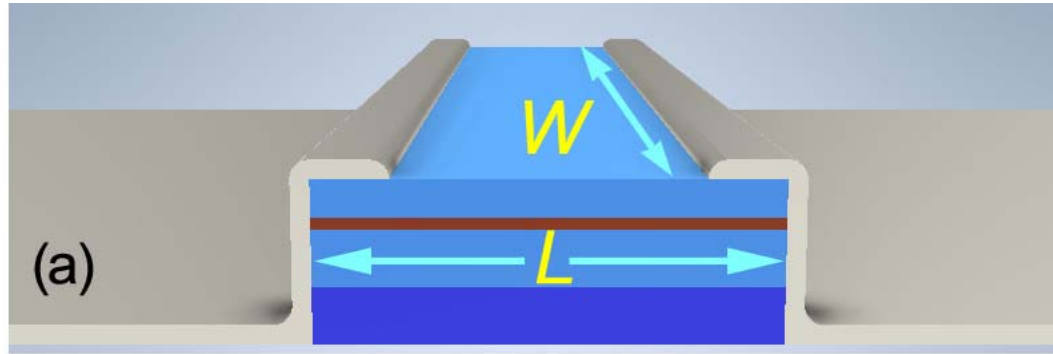
**b**

Hall bar with
top and bottom gates

Lixian Wang, et al. (submitted)

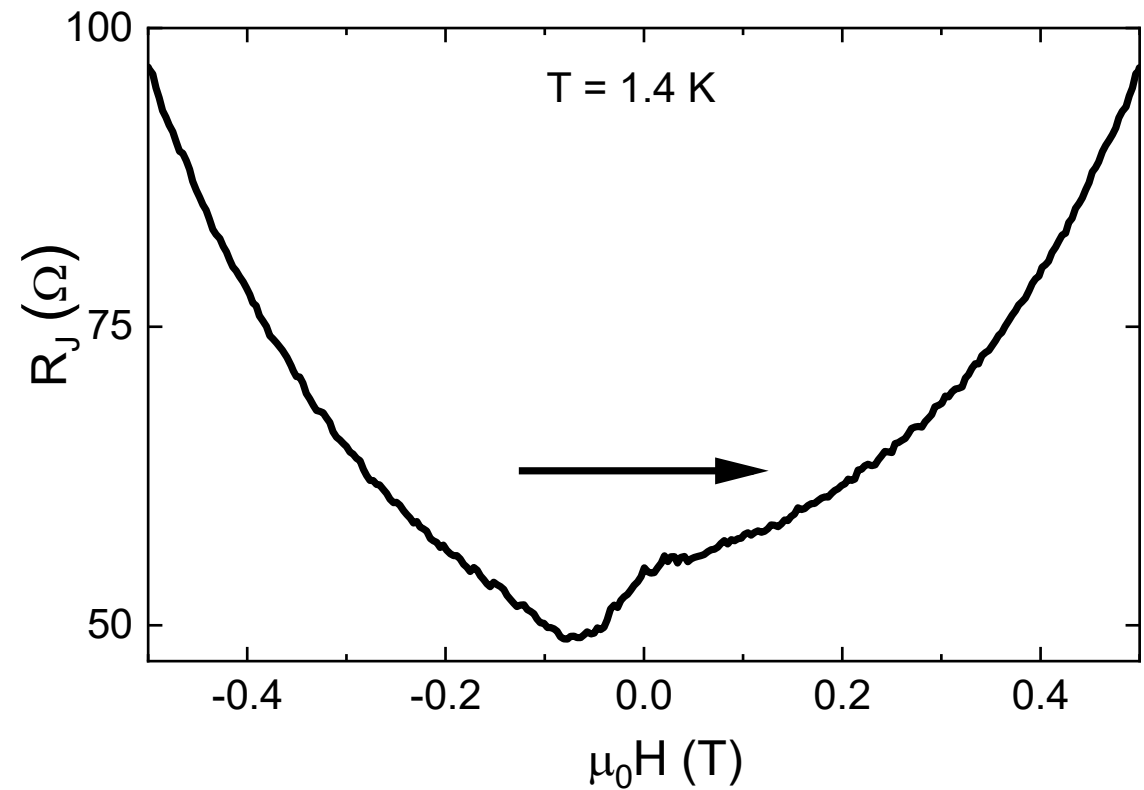
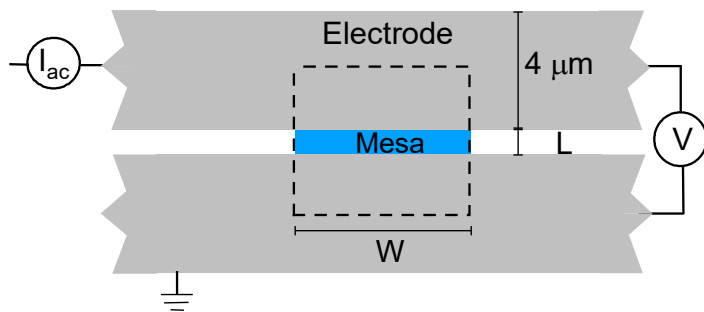


- 11 nm thick quantum well (QW), 2.3% Mn
- With MoRe side-contacted Josephson junction



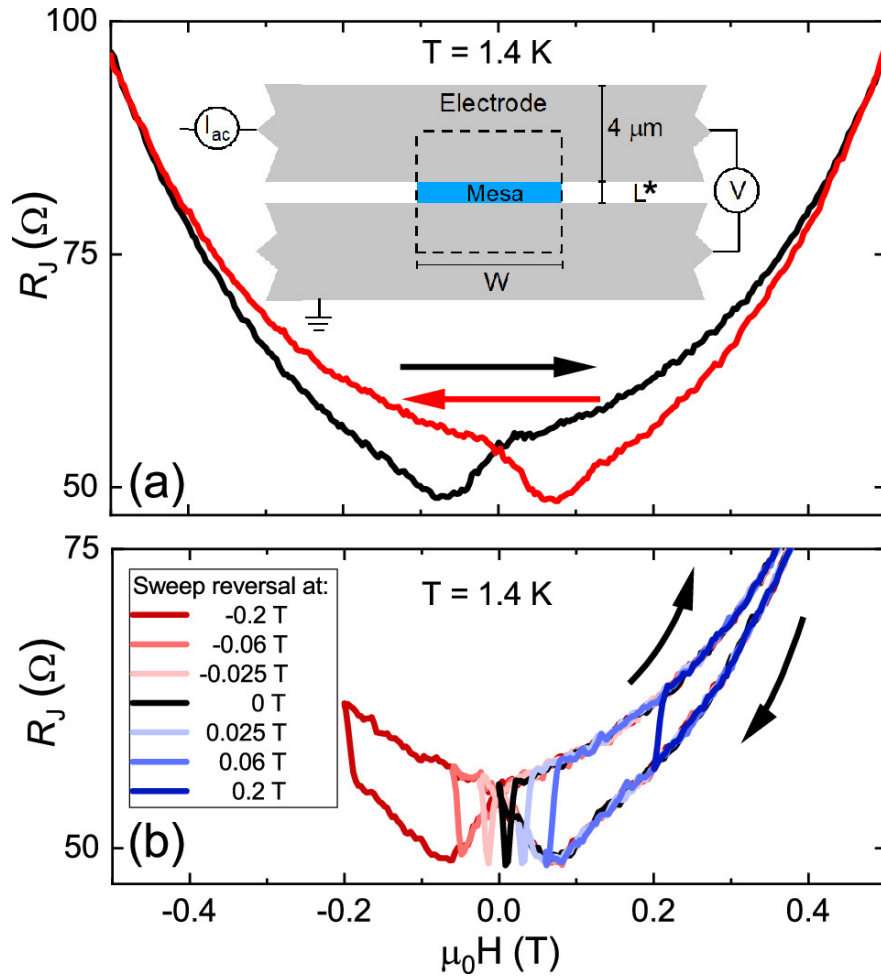
Flux period depends on area of the mesa plus flux focusing area from superconducting leads

With large magnetic field

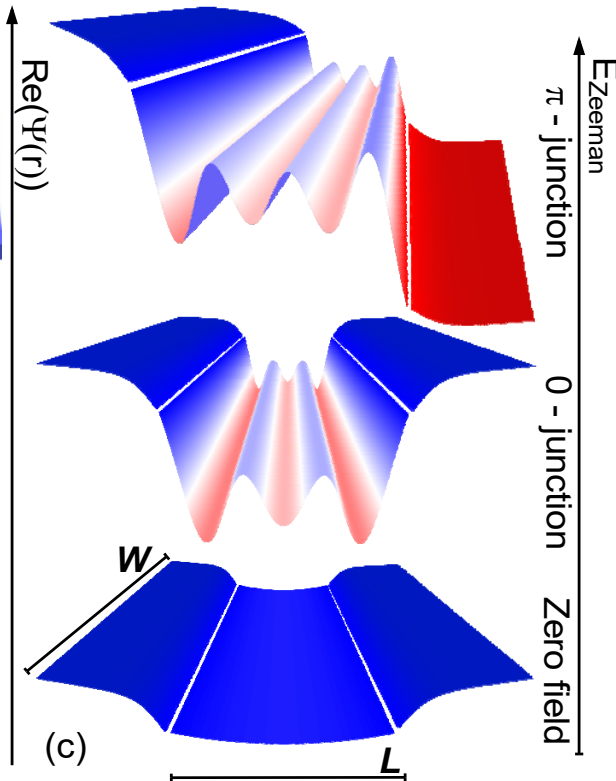
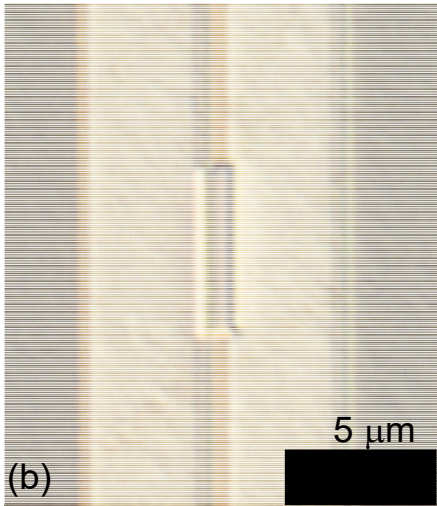
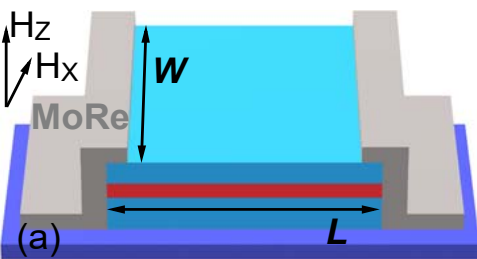


- Quasi 4-terminal measurement of the junction resistance with magnetic field sweep from left, reveals resistance minimum before reaching 0T !?

Flux focusing causes anti-hysteric response at high fields

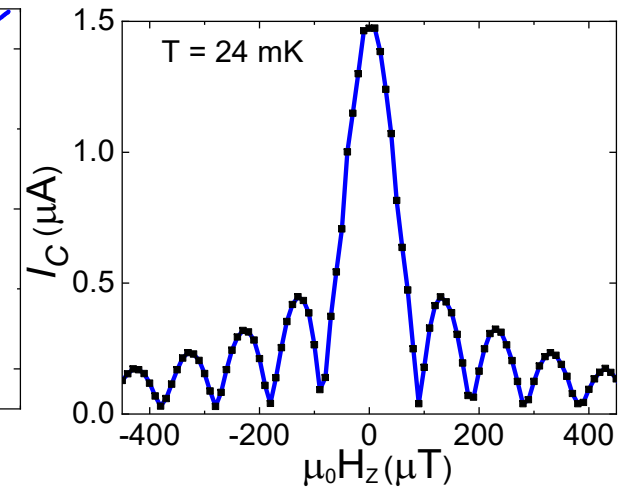
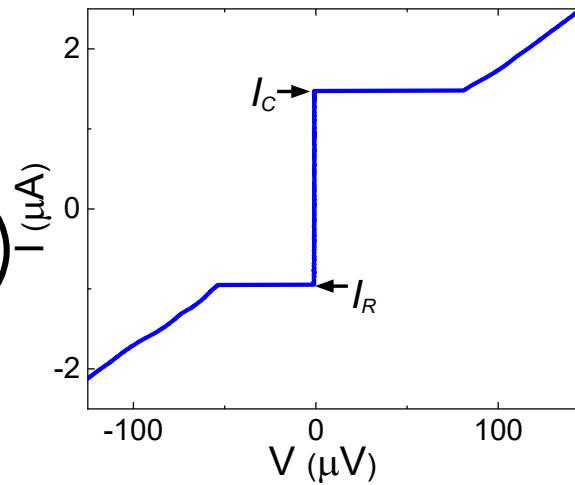
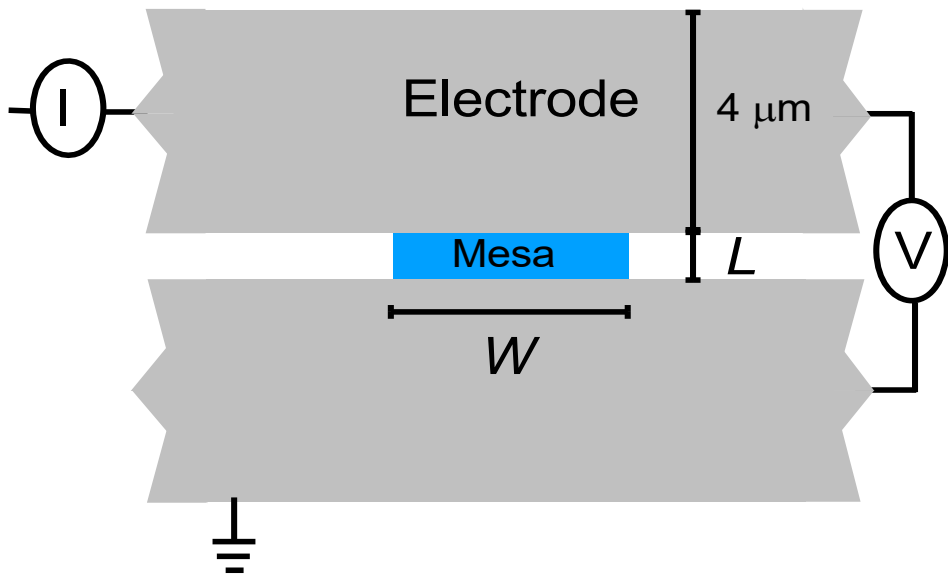


- Junction resistance reveal fields sweep direction dependent magneto-resistance
- Even switching behaviour
- Magnetic hysteresis of type-II superconductor can be understood based on Bean's critical state model from the 1960s



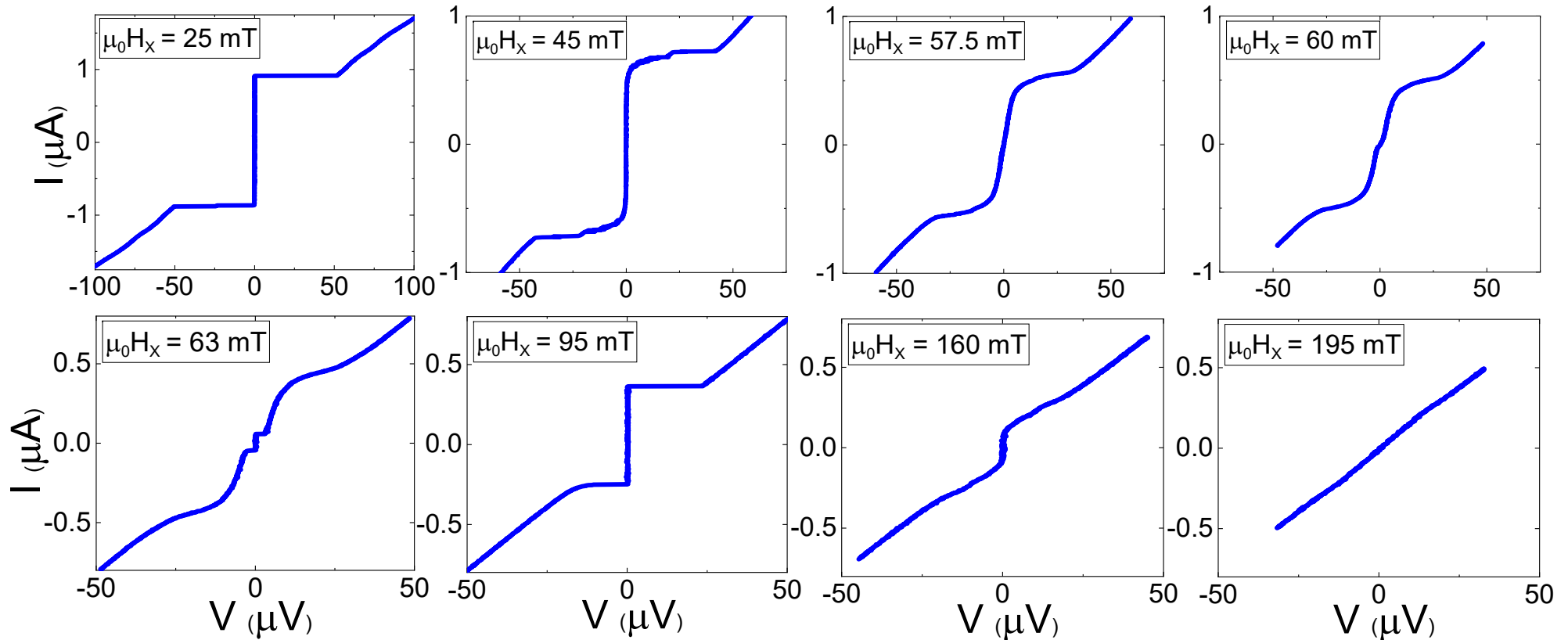
- Fulde-Ferrell-Larkin-Ovchinnikov predicted oscillating order parameter at large Zeeman splitting.
- Plenty large Zeeman in (Hg,Mn)Te

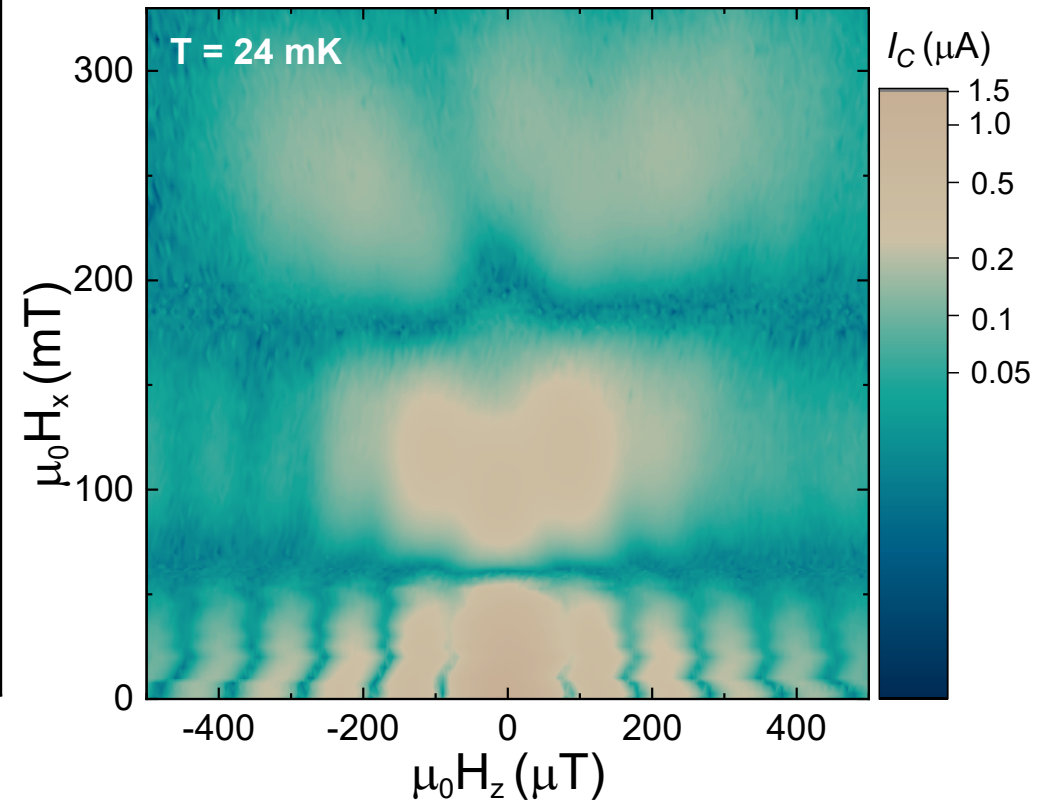
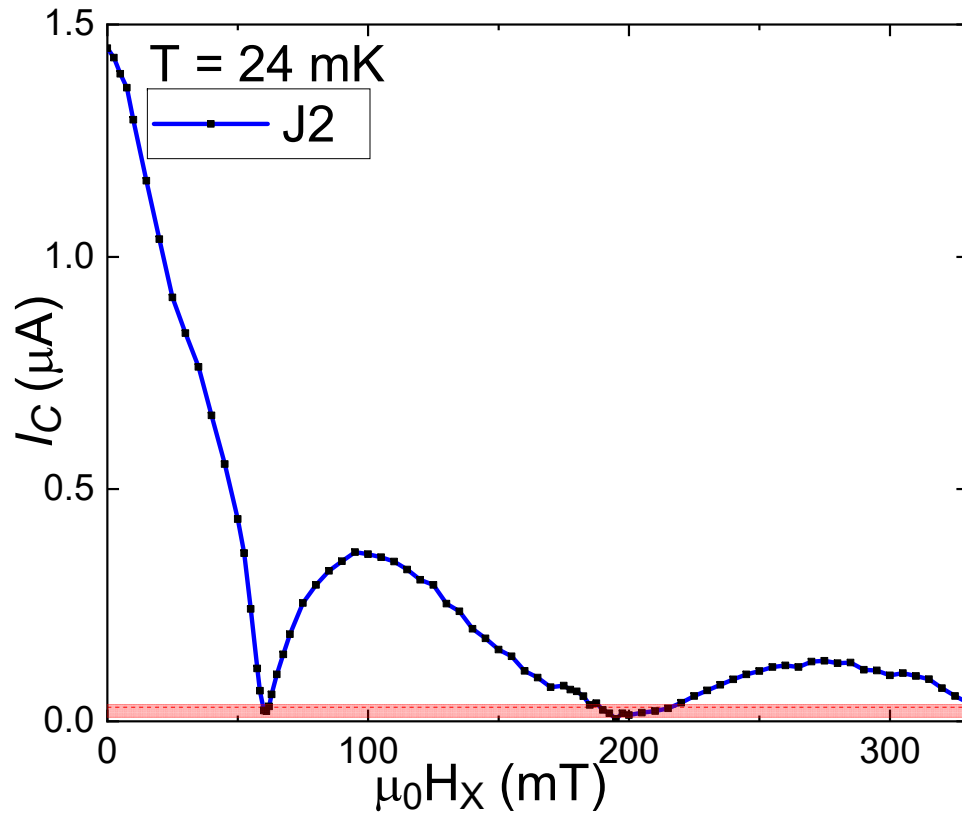
- 11 nm thick quantum well (QW), 2.3% Mn (giant-Zeeman effect)
- QW embedded in (Cd,Hg)Te buffer layer, negligible Rashba spin-orbit coupling
- With MoRe side-contacted Josephson junction
- Device length (L) below bulk mean free path ($1.7 \mu\text{m}$)
- Nomarski image of device
- p-FFLO: Spatially oscillating effective order parameter induced in the QW with increase in Zeeman energy



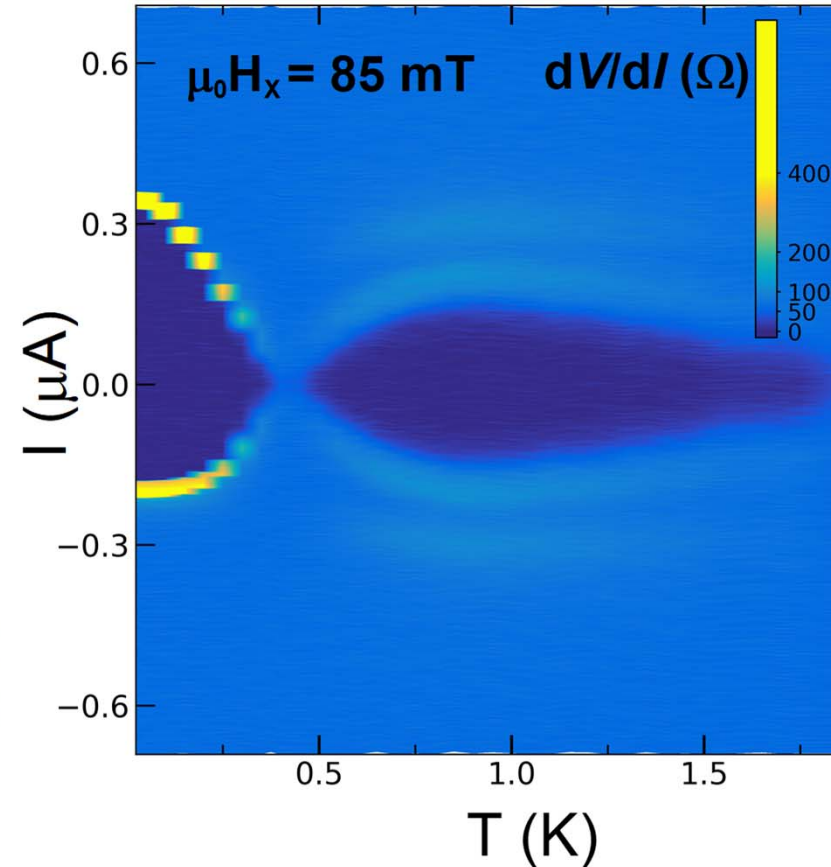
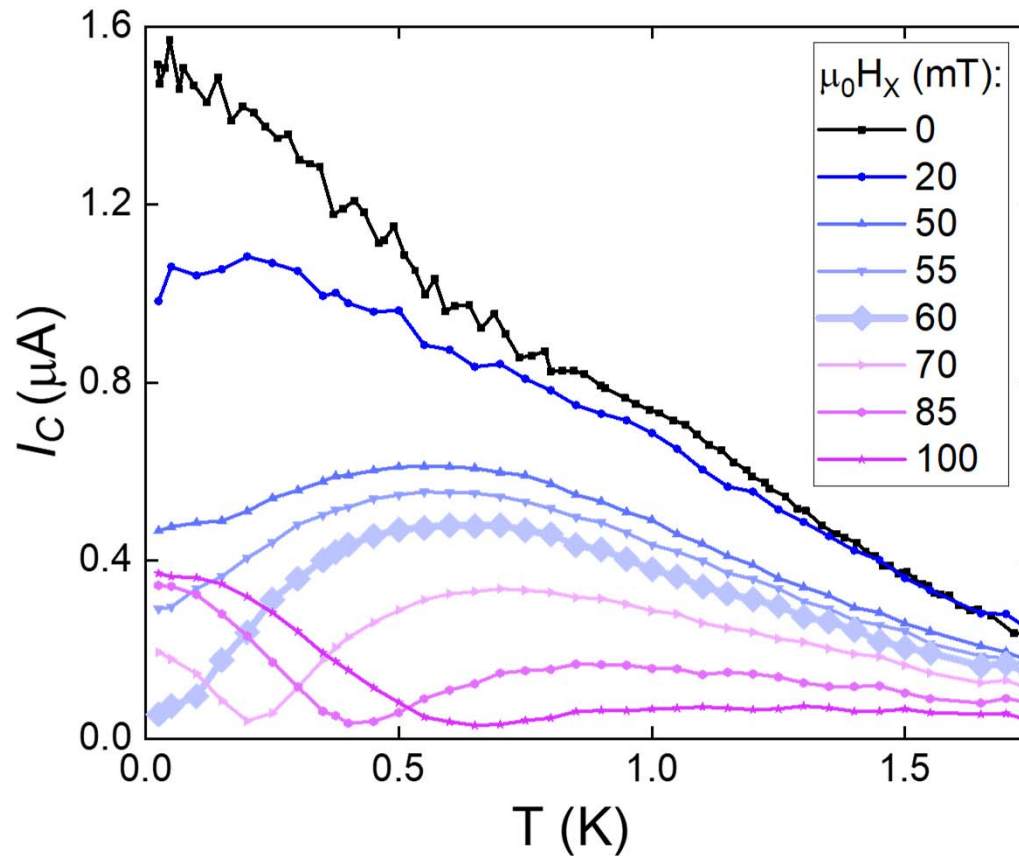
- DC measurement scheme
- $I(V)$ characteristic at zero magnetic field
- I_c extracted using 2 μV voltage criterion
- Fraunhofer pattern $I_c(H_z)$
- H_z below MoRe H_{c1}

I(V) characteristics depend on in-plane field



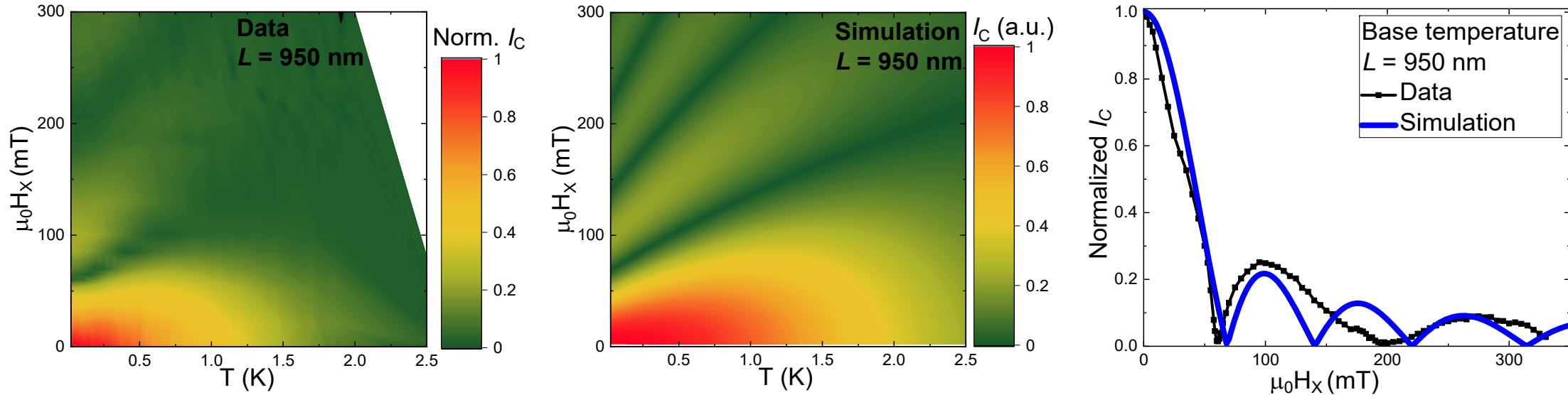


- Red shaded region: 2 μV voltage criterion sets a threshold of 30 nA (for 60 Ω junction resistance) on the I_C sensitivity of the measurement
- I_C goes to zero independent of out-of-plane field



- Giant Zeeman depends on temperature, should show up in temperature dependence of I_c
- We plot temperature dependence of I_c for various in-plane fields
- Reentrance with change in temperature (dark blue area is zero resistance region)

Pankaj Mandal, et al. (submitted)



- Field and temperature dependence of I_C can be modelled based on theory developed for S/F/S junctions [Bergeret et al., PRB **64** (2001)], where exchange field is replaced by Zeeman
- In our case giant-Zeeman effect (E_Z^*) due to interacting Mn atoms resulting in field and temperature dependent Zeeman effect
- Also explains the shifting of the reentrance nodes towards lower fields at lower temperatures

$$E_Z^* = g_0 \mu_B \mu_0 H - \Delta E_{max} B_{5/2} \left[\frac{5g_{Mn} \mu_B \mu_0 H}{2k_B(T + T_0)} \right], \quad I_C \propto T \left| \sum_{\omega > 0} f_s^2 \gamma^2 \frac{\sin(2E_Z^* L / \hbar v_F)}{2E_Z^* L / \hbar v_F} e^{-\frac{L}{l}(1+2\omega\tau)} \right|.$$

- ✓ Quantum spin Hall effect survives Mn doping due to Kondo screening
- ✓ Emergence of $\nu = -1$ quantum Hall state at exceptionally low magnetic fields when chemical potential is in the bulk gap.
- ✓ In 3D device we observe a signature of the parity anomaly.
- ✓ Proximitized layers exhibit (p-)FFLO behaviour.

Collaborators: Pankaj Mandal, Saquib Shamim, Lixian Wang, Wouter Beugeling, Hartmut Buhmann, Charles Gould, Martin Stehno, Ewelina Hankiewicz, Björn Trauzettel
Sebastian Bergeret (San Sebastian), Teun Klapwijk (Delft)

Funding: Freistaat Bayern (ITI), DFG (SFB 1170, ct.qmat CoE), EU-ERC AGs “3 -TOP”, “4 TOPS”,